

# Radar detection of high-energy neutrino induced particle cascades in ice

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IIHE

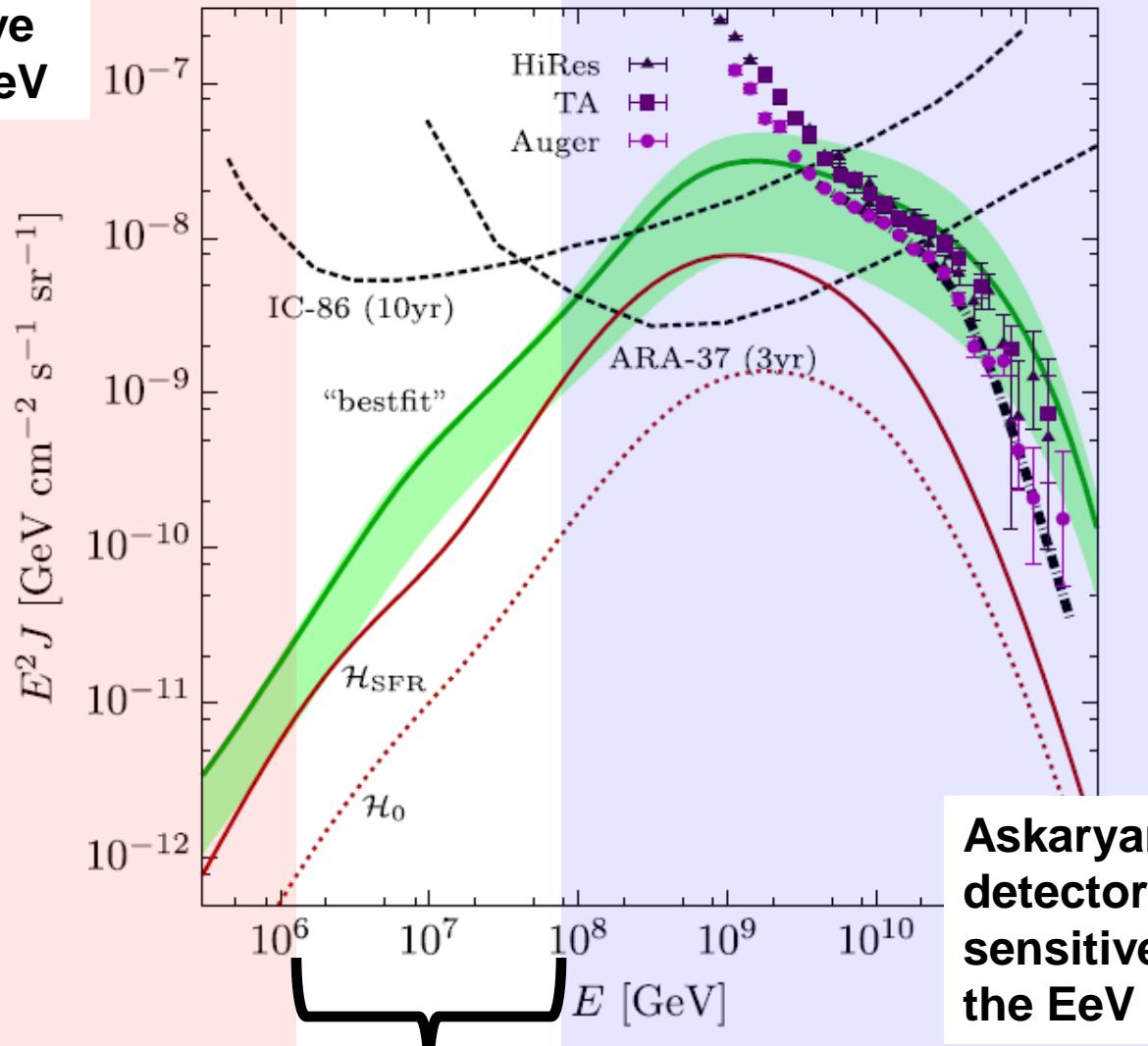
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UW -Madison <sup>2</sup>

Université Libre de Bruxelles <sup>3</sup>

# Motivation

IceCube sensitive  
below several PeV

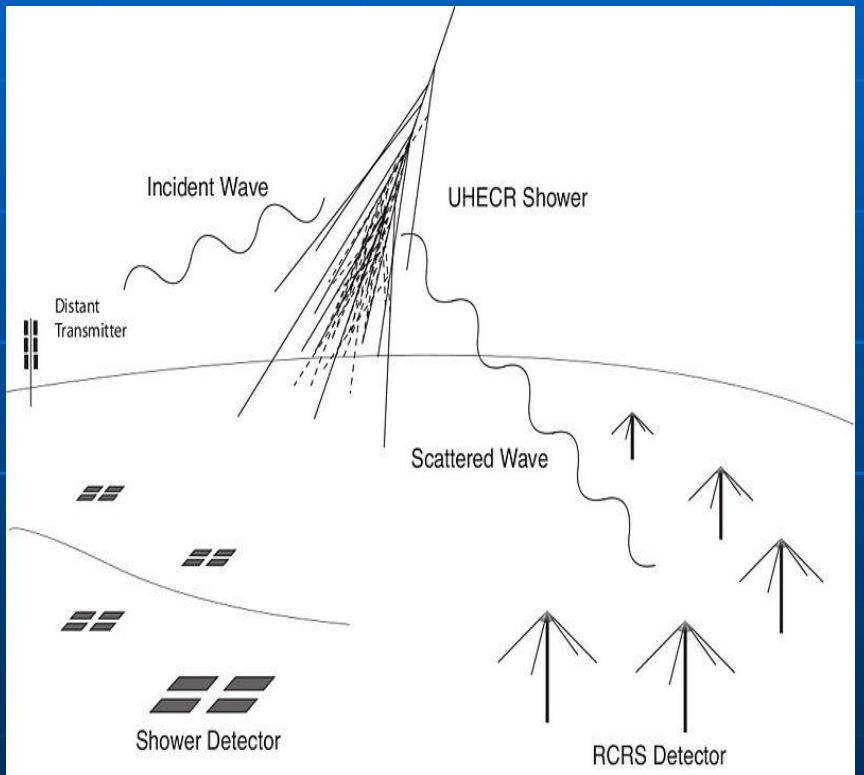


Askaryan Radio  
detectors become  
sensitive close to  
the EeV region

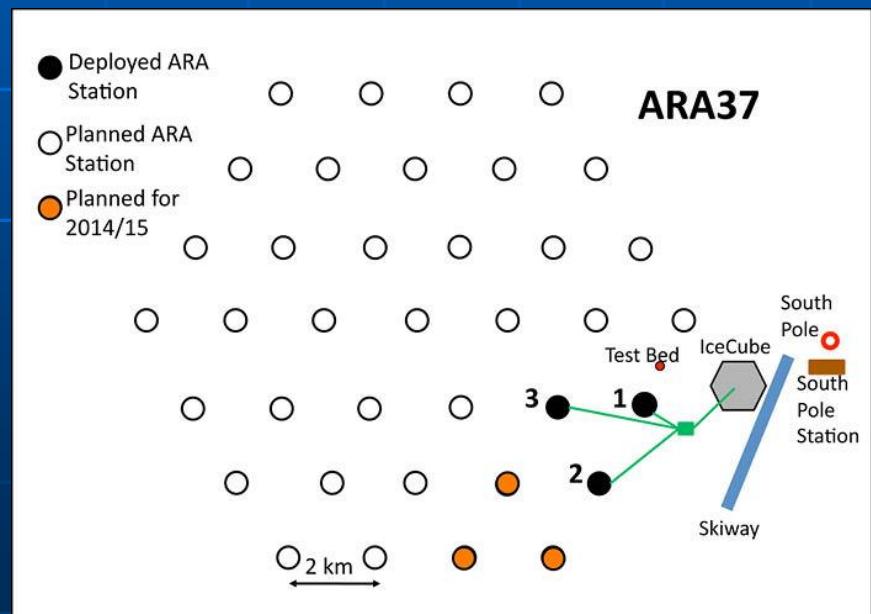
Sensitivity Gap in  
PeV – EeV region

# New detection method

If a RADAR signal can be bounced off of a neutrino induced cascade in ice, we have **control over the signal strength!**



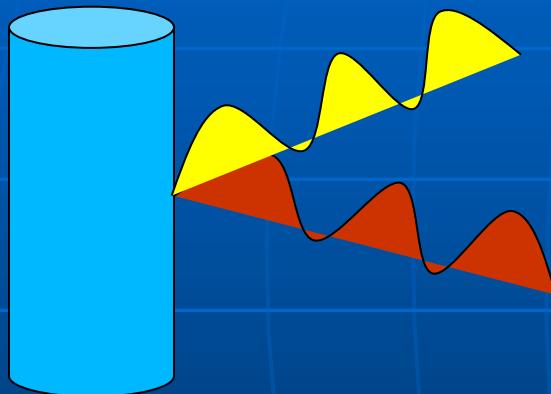
**Infrastructure already available!**



M. Abou Bakr Othman et al,  
Proceedings 32nd ICRC, Beijing 2011

# RADAR scattering

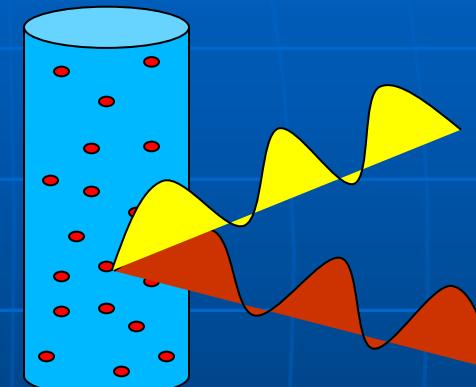
- Over-dense scattering:



Radar frequency < Plasma Frequency

Reflection from the surface of the plasma tube

- Under-dense scattering:

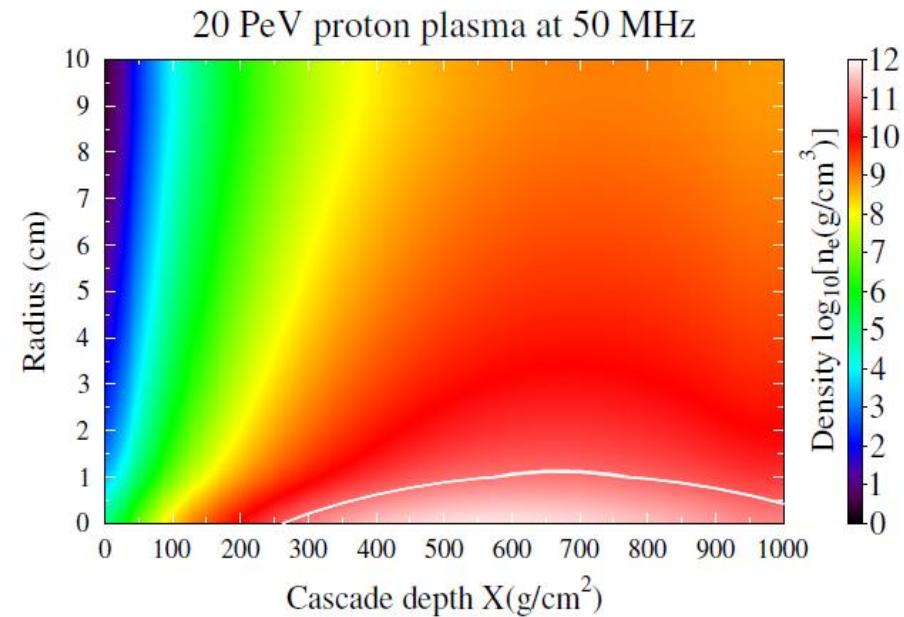
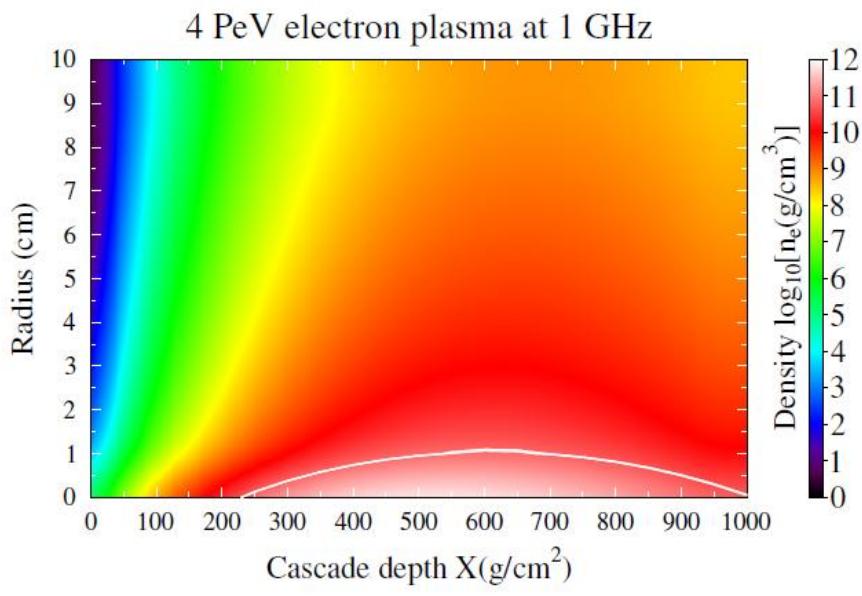


Radar frequency > Plasma Frequency

Scattering off of the individual charges in the plasma

# Over-dense scattering

$$\mathcal{V}_{Plasma} > \mathcal{V}_{Radar} > \begin{cases} 1/\tau_{Plasma} & c_{med}\tau_e < l_c \\ c_{med}/l_c & c_{med}\tau_e > l_c \end{cases}$$
$$\mathcal{V}_{Plasma} \propto \sqrt{n_{Plasma}} \propto \sqrt{E_{primary}}$$



# RADAR return power estimation

## Bi-static RADAR configuration

Effective area of receiver:  $A_{\text{eff}}$

Re-scattering over a sphere:  $1/(4\pi R^2)$

Plasma scattering surface:  $\sigma_{\text{eff}}$

Transmitted power:  $P_t$

Transmission over  $\frac{1}{4}$  of a sphere:  $1/(\pi R^2)$

Attenuation by the medium

$$P_r = P_t \eta \frac{\sigma_{\text{eff}}}{\pi R^2} \frac{A_{\text{eff}}}{4\pi R^2} e^{-4R/L_\alpha}$$

# RADAR return power estimation (single antenna)

$$P_r = P_t \eta \frac{\sigma_{eff}(\lambda) A_{eff}(\lambda)}{\pi R^2} \frac{4\pi R^2}{4\pi R^2} e^{-4R/L_\alpha}$$

$$\lambda = 0.18 \text{ m}$$

$$\sigma_{eff}^{max} = 0.11 \text{ m}^2$$

$$\sigma_{eff}(\theta = 60^\circ, \phi = 60^\circ) = 1.6 \cdot 10^{-4} \text{ m}^2$$

$$L_\alpha = 1 \text{ km}$$

$$P_{noise} = k_b T_{sys} \Delta \nu$$

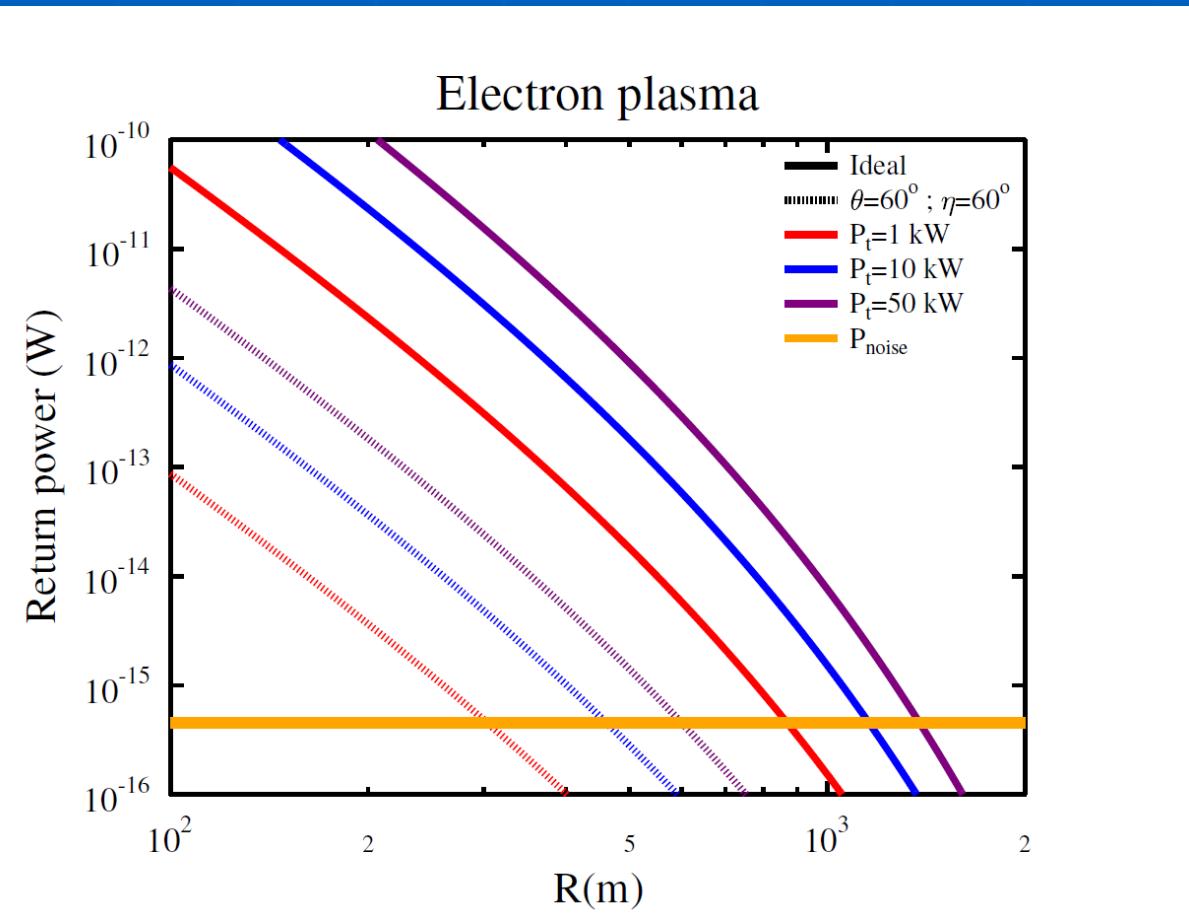
$$T_{sys} = 325 \text{ K}$$

$$\Delta \nu = 100 \text{ kHz}$$

N antennas :

$$P_{Noise}(N) = N \cdot P(N=1)$$

$$P_{Signal}(N) = N^2 \cdot P(N=1)$$



# RADAR return power estimation (single antenna)

$$P_r = P_t \eta \frac{\sigma_{eff}(\lambda) A_{eff}(\lambda)}{\pi R^2} \frac{4\pi R^2}{4\pi R^2} e^{-4R/L_\alpha}$$

$$\lambda = 3.6 \text{ m}$$

$$\sigma_{eff}^{max} = 5.5 \text{ m}^2$$

$$\sigma_{eff}(\theta = 60^\circ, \phi = 60^\circ) = 1.2 \cdot 10^{-2} \text{ m}^2$$

$$L_\alpha = 1.4 \text{ km}$$

$$P_{noise} = k_b T_{sys} \Delta \nu$$

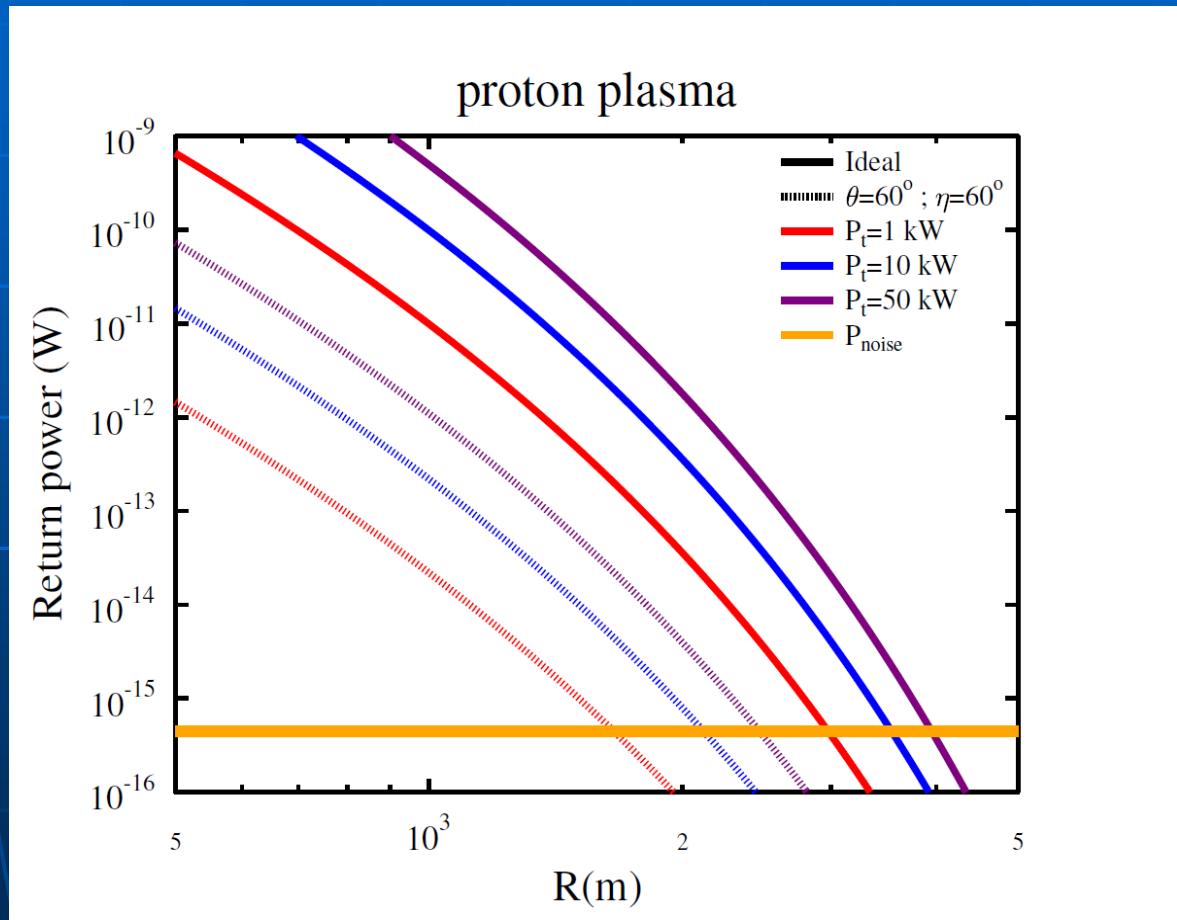
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# RADAR return power estimation (single antenna)

$$P_r = P_t \eta \frac{\sigma_{eff}(\lambda) A_{eff}(\lambda)}{\pi R^2} \frac{4\pi R^2}{4\pi R^2} e^{-4R/L_\alpha}$$

$$\lambda = 3.0 \text{ m}$$

$$\sigma_{eff}^{max} = 5.5 \text{ m}^2$$

$$\sigma_{eff}(\theta = 60^\circ, \phi = 60^\circ) = 1.2 \cdot 10^{-2} \text{ m}^2$$

$$L_\alpha = 1.4 \text{ km}$$

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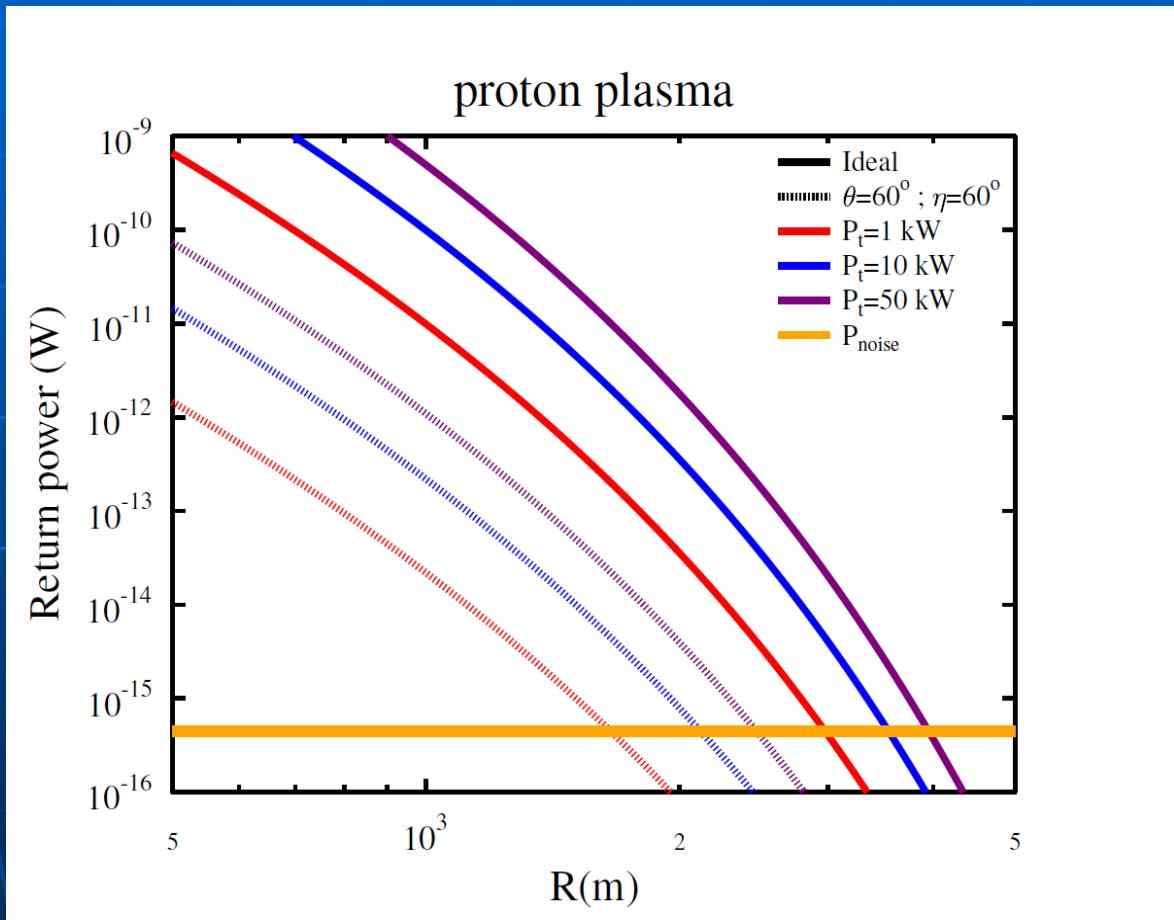
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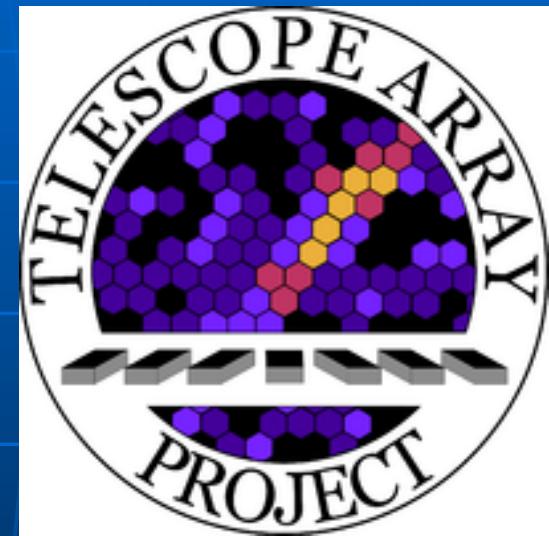
# **Open questions: The Plasma**

- How large is the over-dense plasma?
- What is the influence of skin-effects?
- What is the lifetime of the plasma?
- Is the plasma collision frequency low enough?



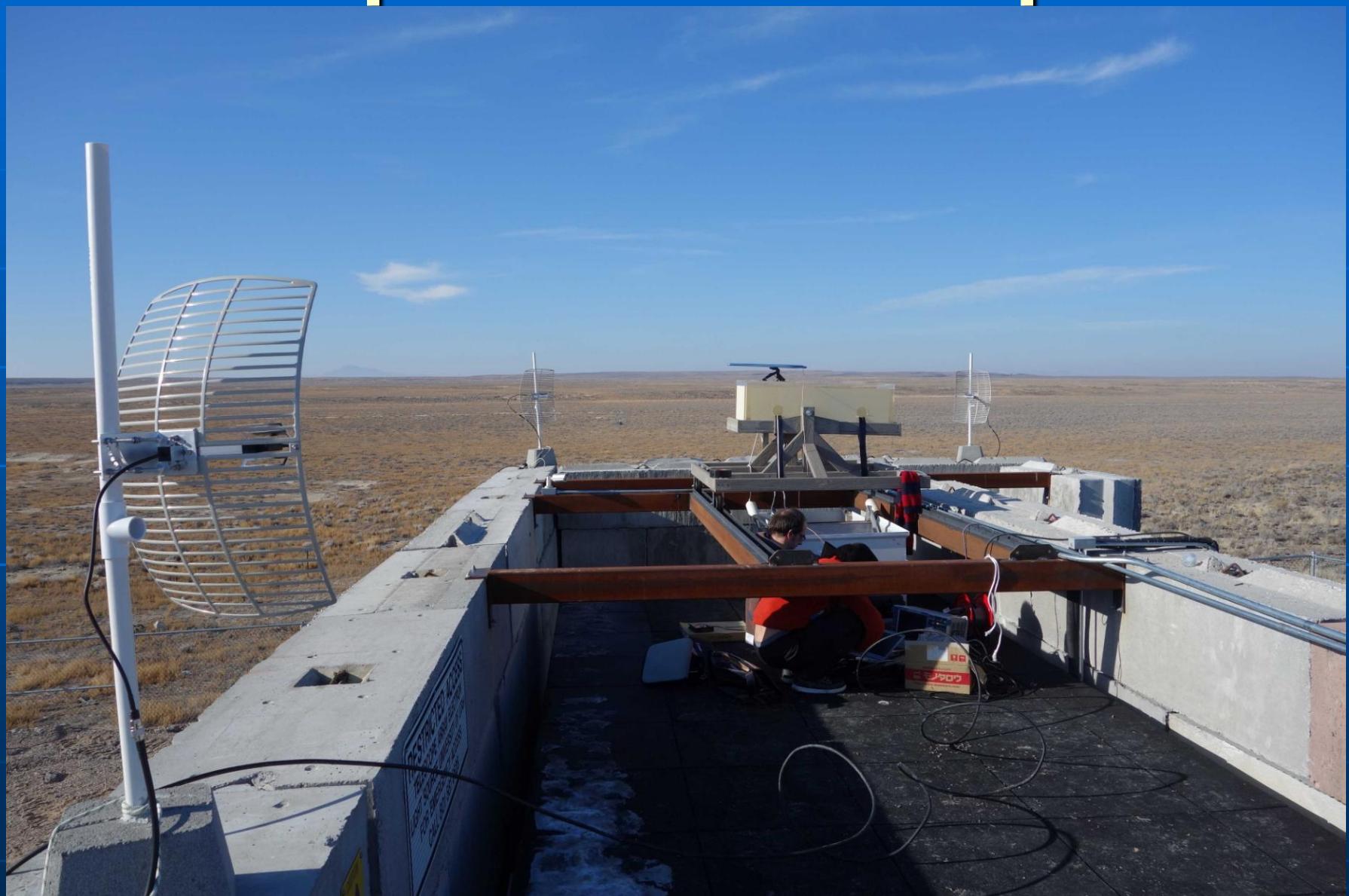
**Experimental verification  
needed!**

# Radar scattering experiment at TA-ELS

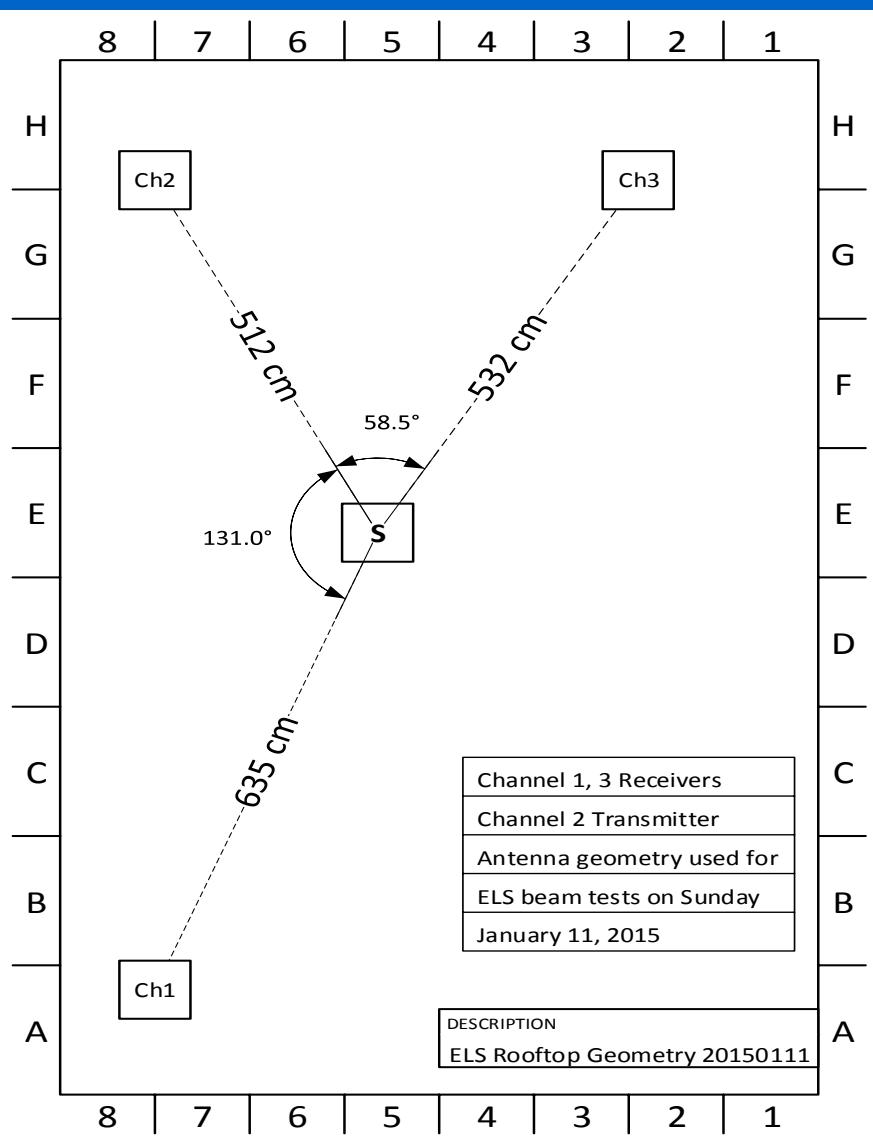


Many thanks to the Chiba group and  
the Telescope Array Collaboration !

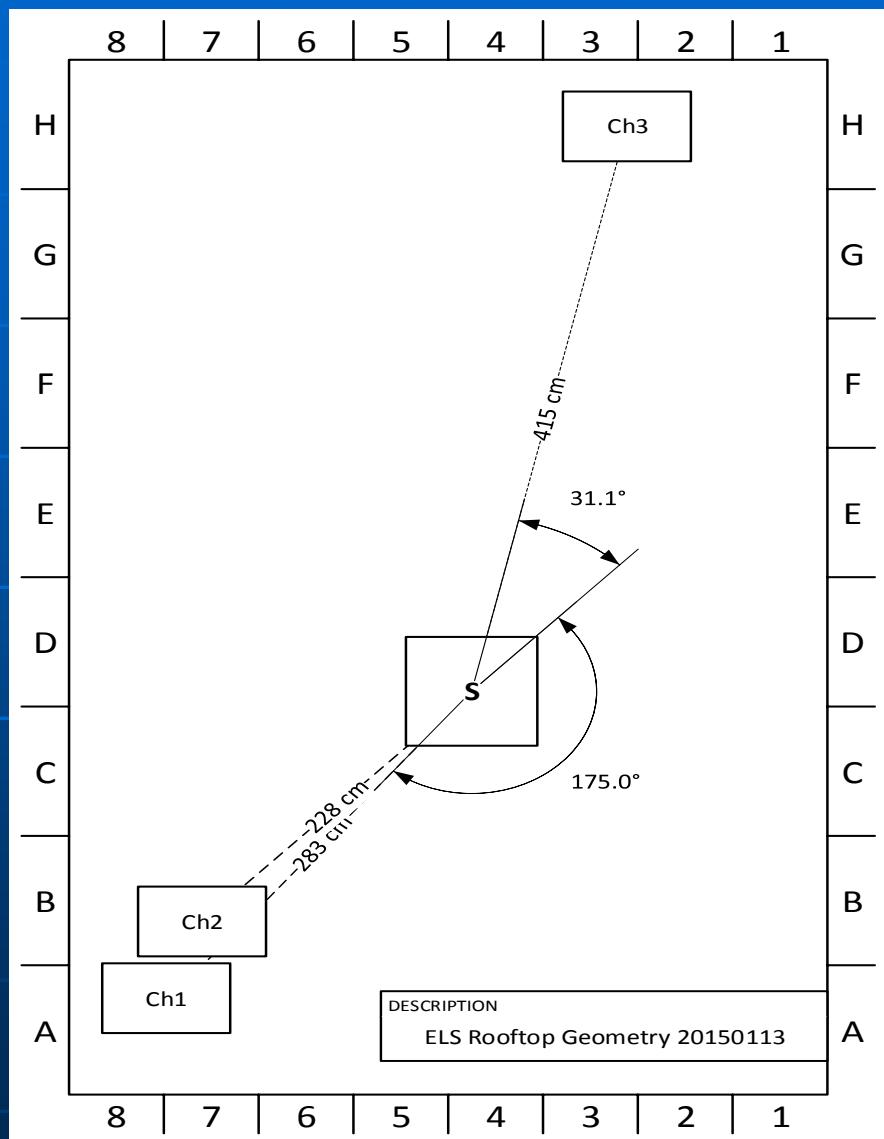
# Experimental setup



# Experimental setup

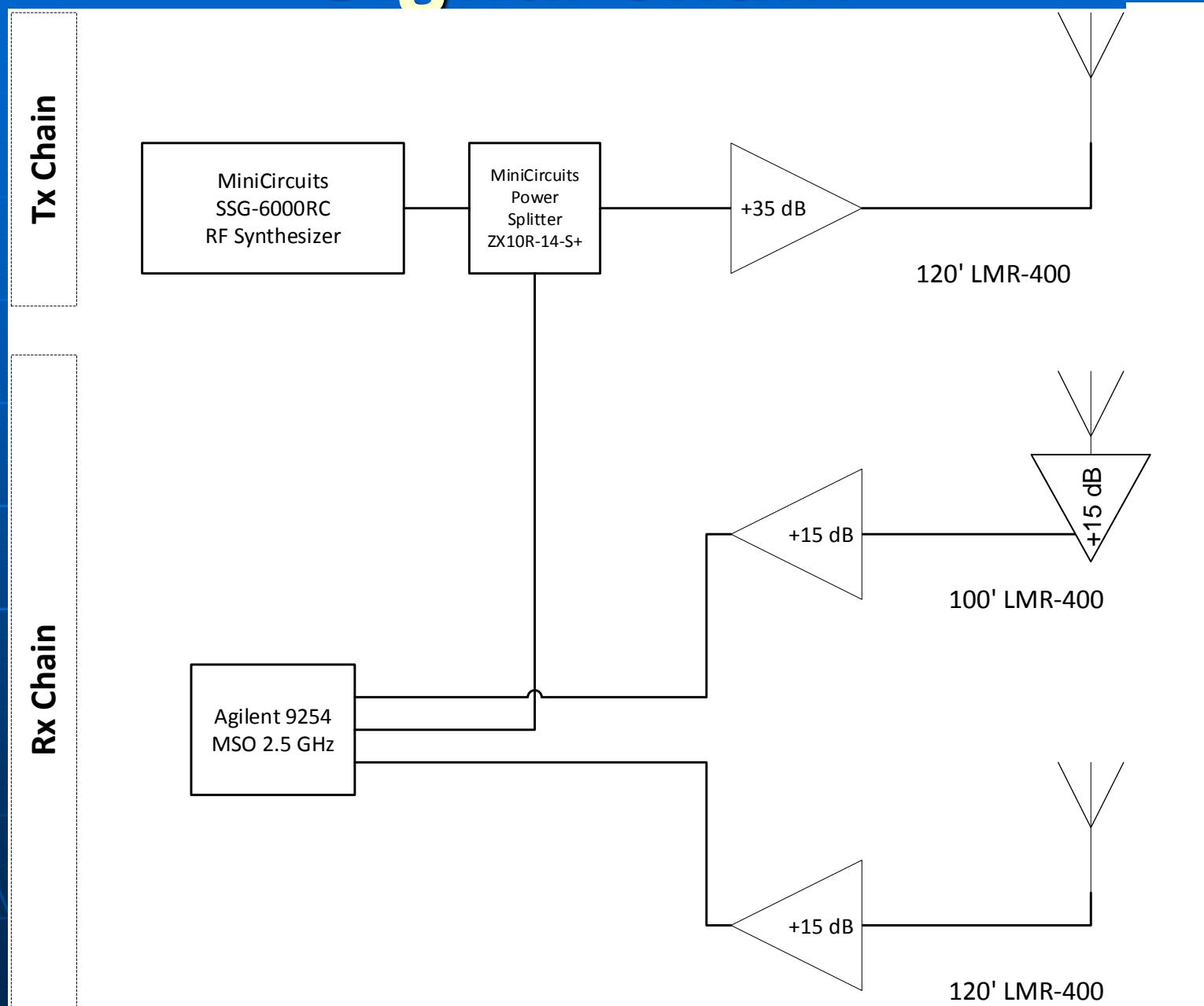


Early Configuration

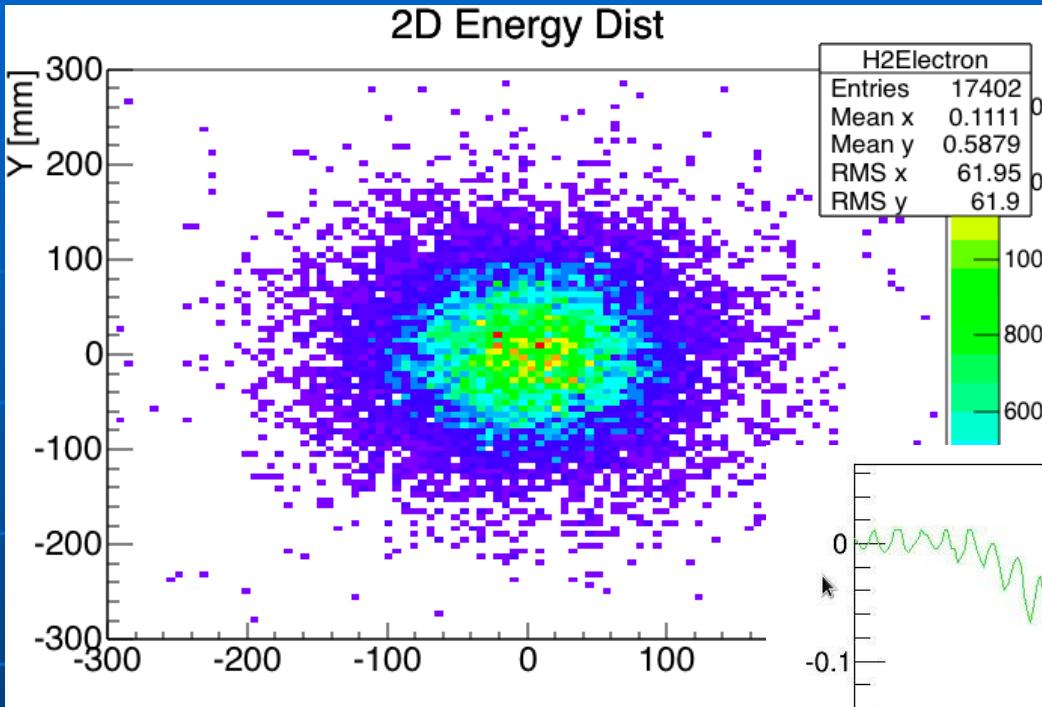


Later Configuration

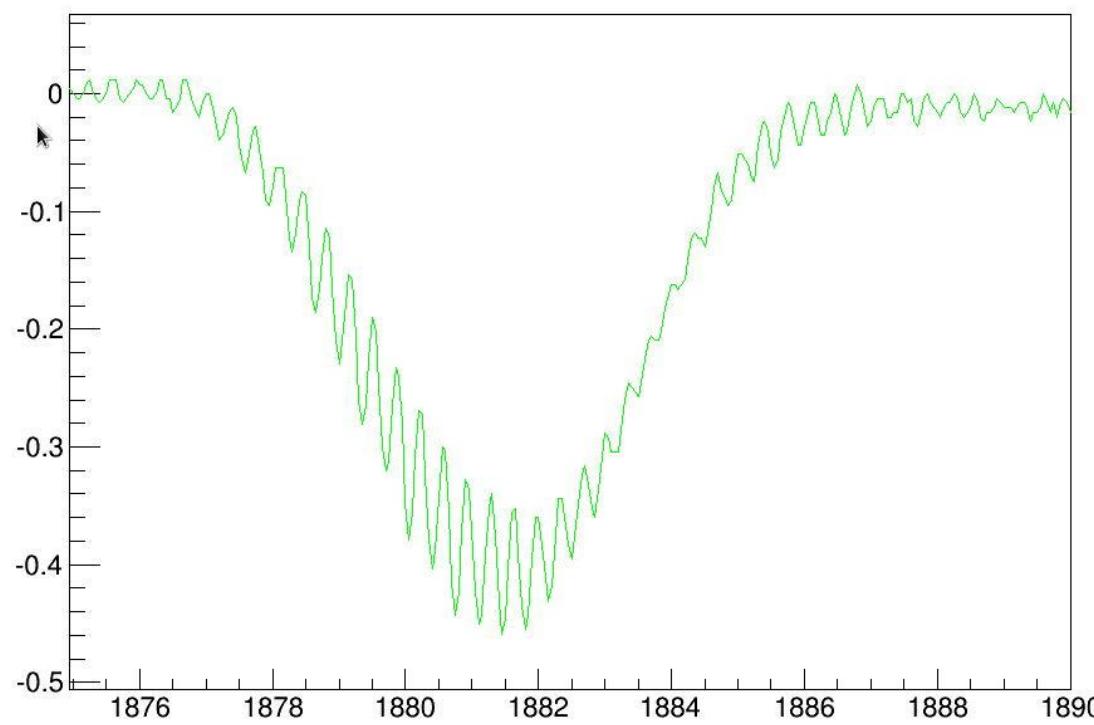
# Signal chain



# Radar scattering Beam characteristics

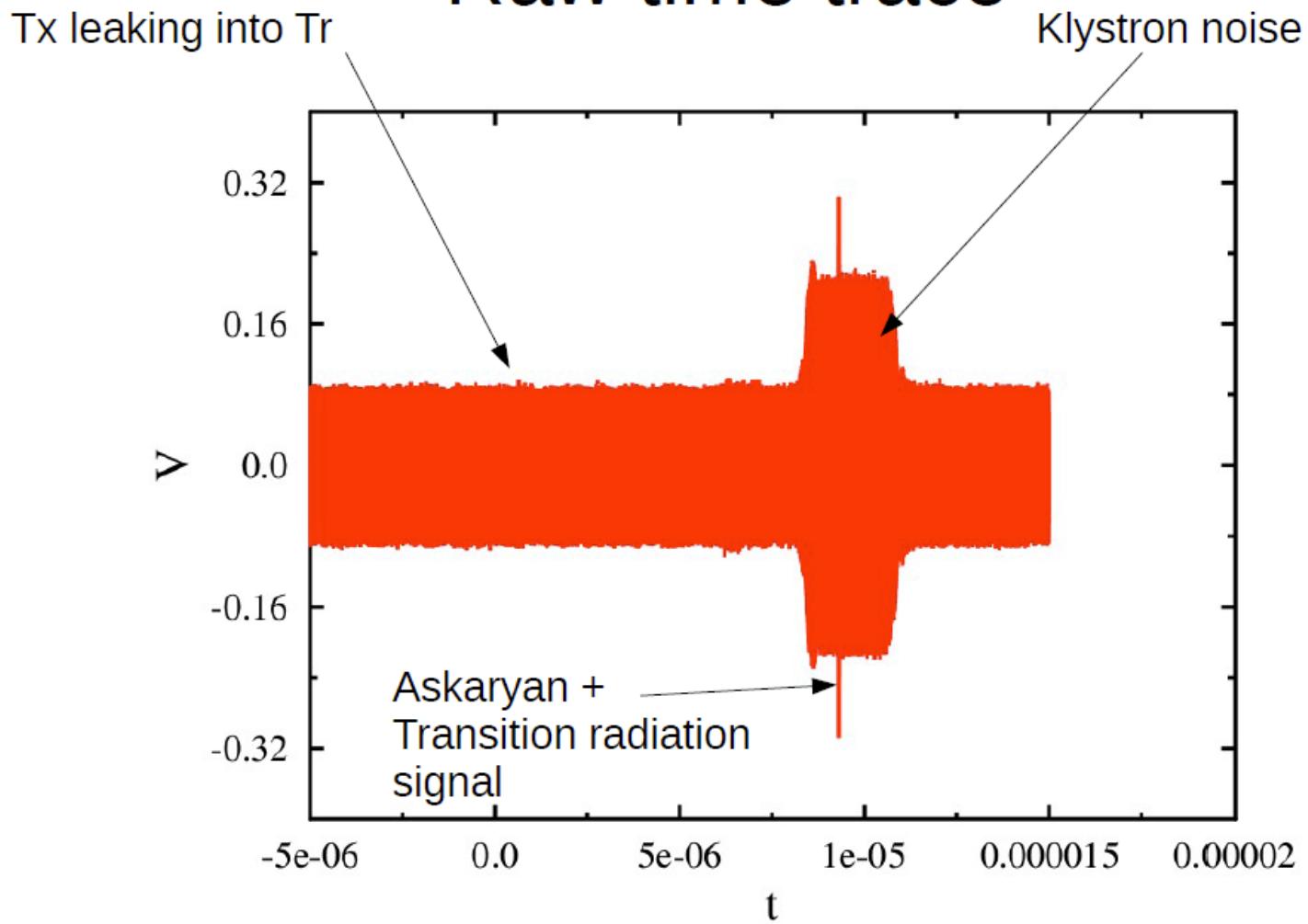


~ $10^9$  (40 MeV) electrons  
~ 40 PeV

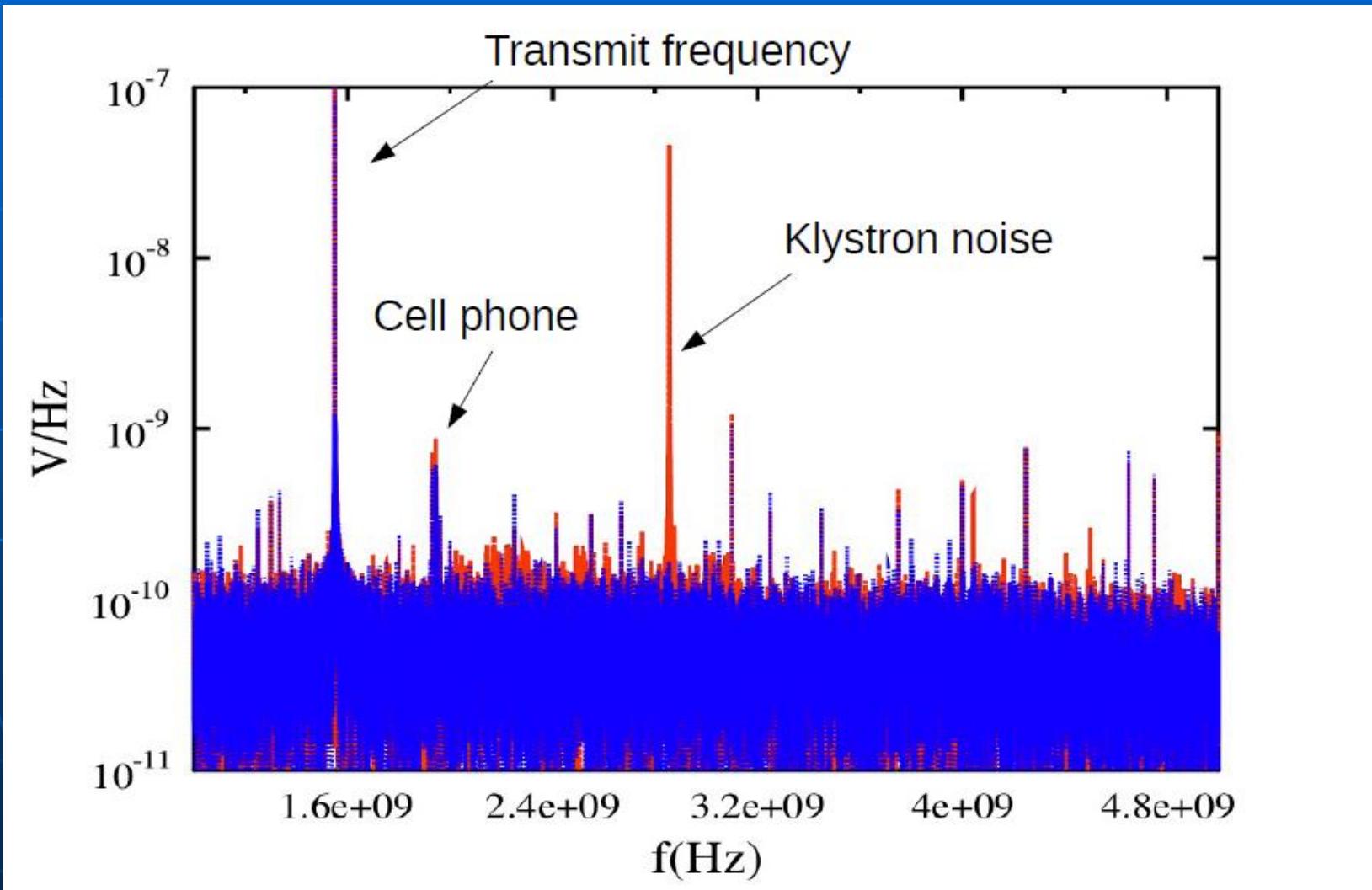


# Radar scattering What do we see?

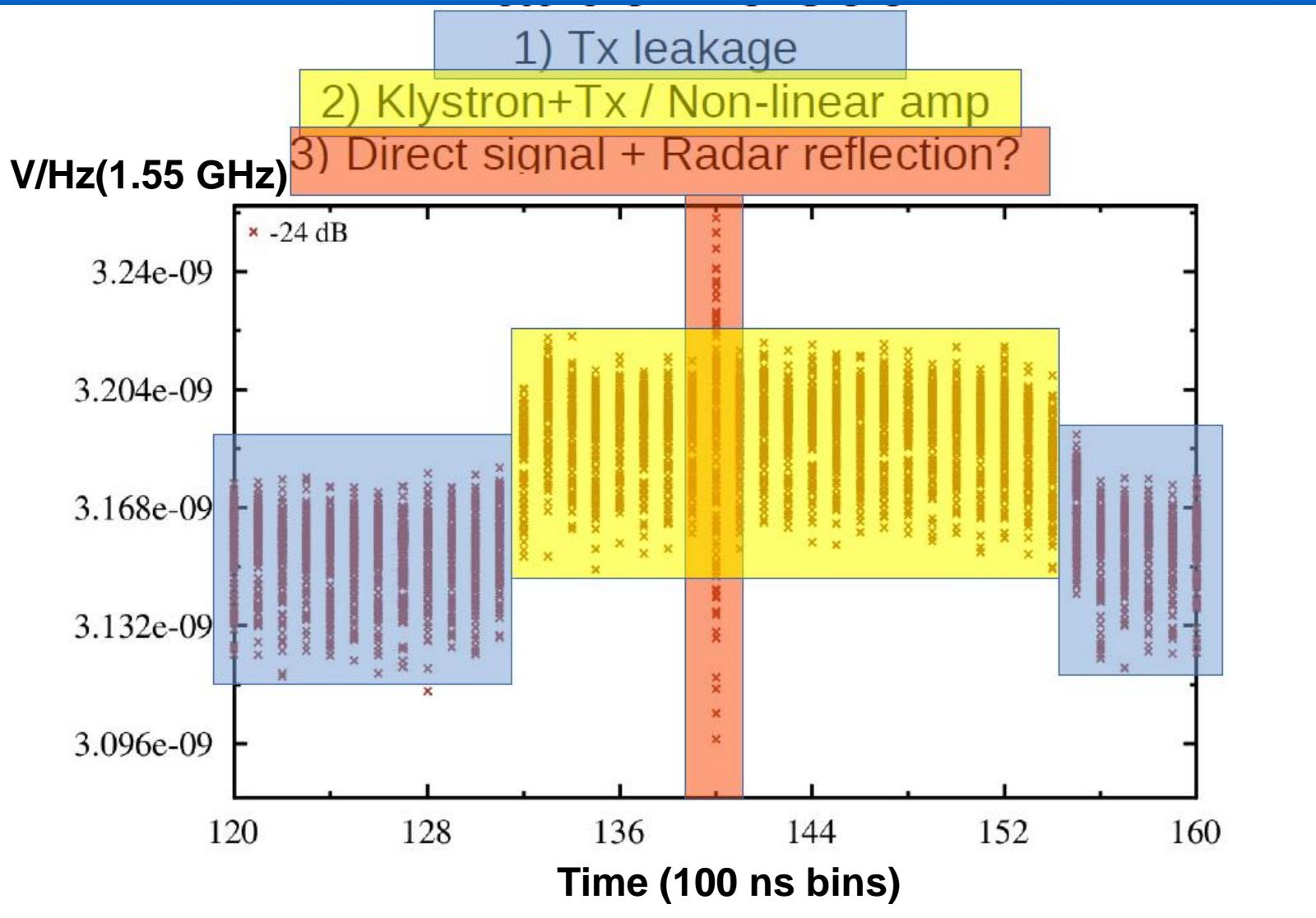
Raw time trace



# Radar scattering What do we see?



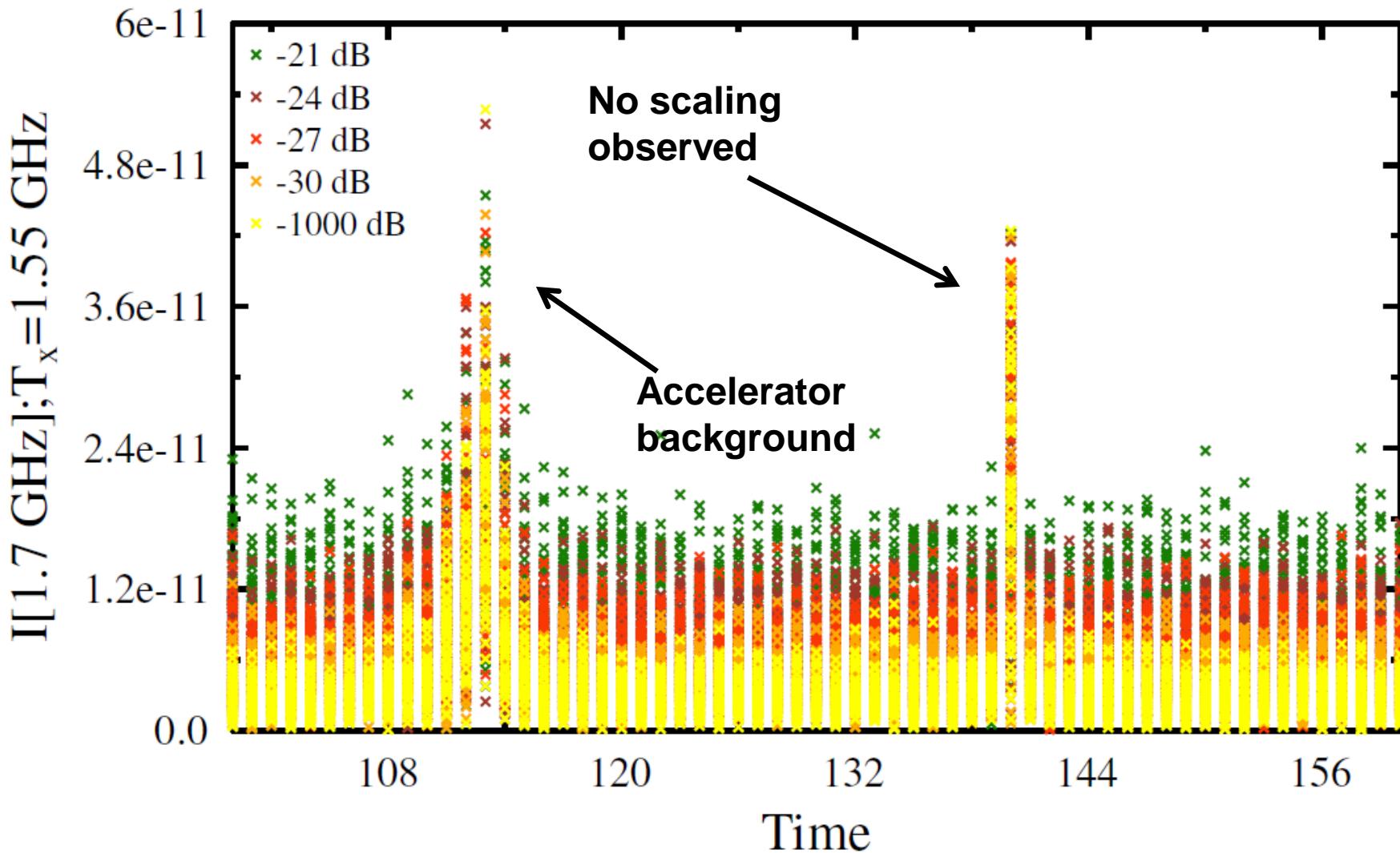
# Radar scattering What do we see?



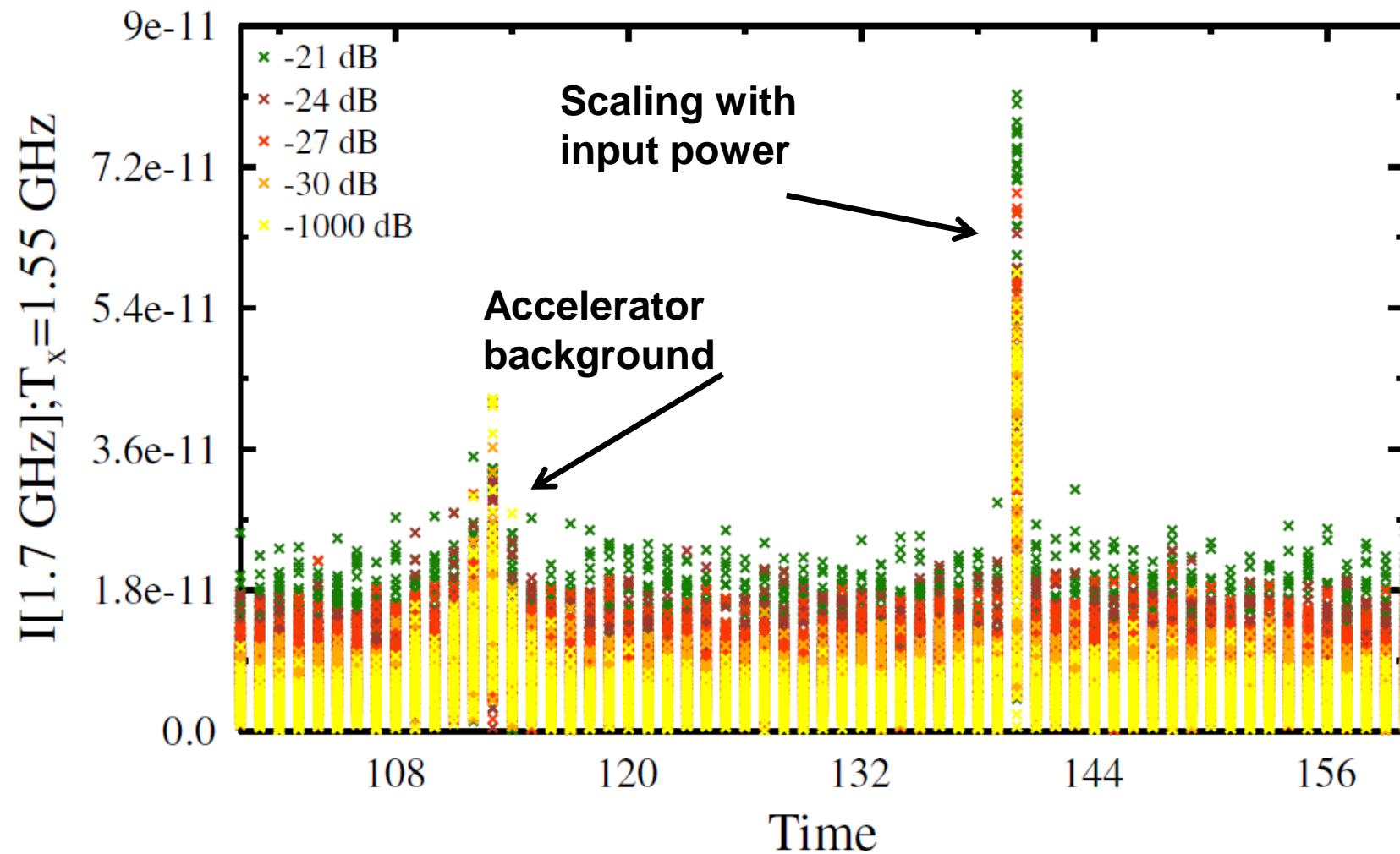
# Radar scattering Interference and instrumental effects

- Accelerator noise interferes with our transmit signal
- Non-linear amplifier response
- Signal can be mimicked by these effects!
- What if we look at a different frequency than our transmit frequency?

# Radar scattering Air



# Radar scattering ice



# Conclusions

- Modeling the RADAR scattering of high-energy neutrino induced cascades gives an energy threshold of **several PeV**.
- We performed a measurement to determine the feasibility of this method.
- Obtained data **hints toward a scattered signal, analysis is ongoing**.

# Three different types of plasma are considered

Leftover electrons from ionization:

Extension:  $O(30 \text{ cm})$

Lifetime:  $O(1-20 \text{ ns})$

Shower front electrons:

Extension:  $R_L = O(10 \text{ cm})$

Lifetime:  $O(100\text{ns})$

Moving!

Leftover protons from ionization:  
Wide extension:  $O(5\text{m})$   
Lifetime:  $O(10-1000 \text{ ns})$

Ionization numbers come from Physical Chemistry research!

6. Laws, J. O. & Parsons, D. A. EOS 24, 452–460 (1943).

Proton mobility in ice

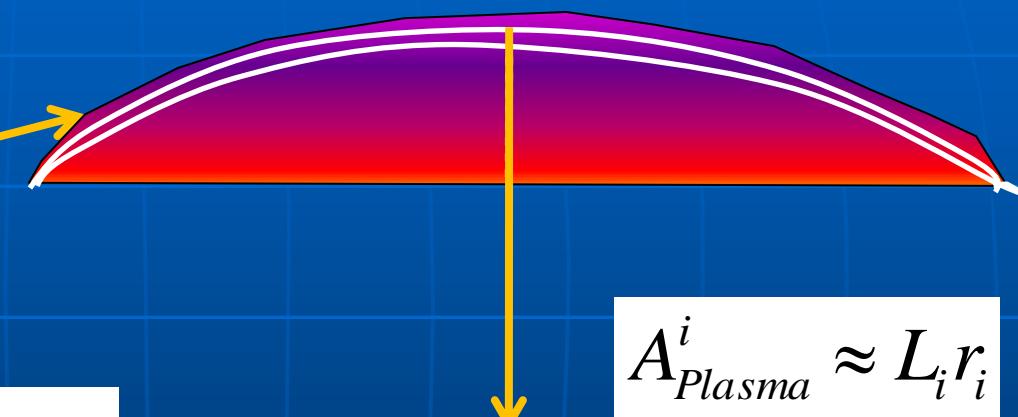
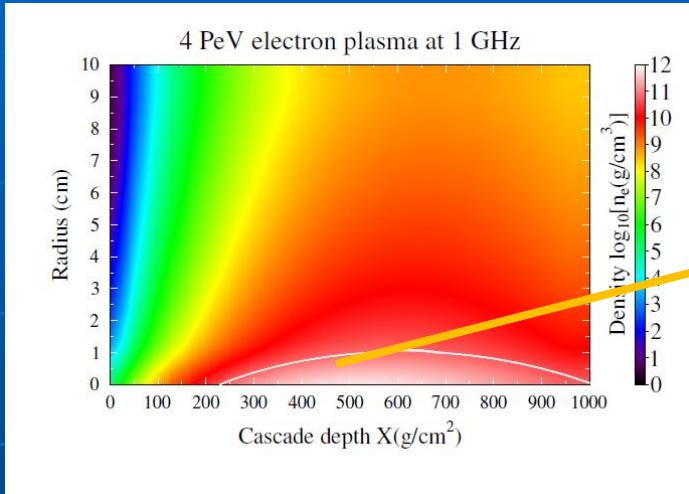
Marinus Kunst & John M. Warman

Interuniversitair Reactor Instituut, Mekelweg 15, 2629 JB Delft,  
The Netherlands

Ice is frequently taken as a model when factors controlling proton transport in hydrogen-bonded molecular networks are discussed. Such discussions have increased with the acknowledgement that proton transfer across cell membranes may play a significant part in energy conversion and storage in biological systems<sup>1–4</sup> and that this transfer may involve hydrogen-bonded chains spanning the membrane<sup>5,6</sup>. However, there is still much

# Skin Effects

Model: Consider over-dense cylinders of equal density



Calculate skin depth  
for a collision less plasma:

$$\delta = \frac{c}{2\omega_p}$$

Within 1 skin depth the  
amount of power absorbed  
and re-scattered equals:

$$f_{skin}^{i+1} = (1 - f_{skin}^i)(1 - e^{-\frac{x}{\delta_i}})$$

$$A_{Plasma}^i \approx L_i r_i$$

$\approx$

# The over-dense radar cross-section

This approach:

1. Include skin-effects directly into the radar cross-section.
2. Consider projected area and polarization angles for in/out-going wave

$$\sigma_{od} = A_{plasma} \times f_{skin} \times f_{geom}$$

$$A_{Plasma}^i \approx L_i r_i$$

$$f_{skin}^{i+1} = (1 - f_{skin}^i)(1 - e^{-x/\delta_i})$$

$$f_{geom} = (\vec{e}_t \cdot \vec{e}_c)(\vec{e}_c \cdot \vec{e}_r)$$

$$\sigma_{od} = \sum_i L_i r_i (1 - f_{skin}^i)(1 - e^{-x/\delta_i})(\vec{e}_t \cdot \vec{e}_c)(\vec{e}_c \cdot \vec{e}_r)$$

# The under-dense radar cross-section

The wave will scatter off of the individual electron given by the Thompson cross-section

$$\sigma_T = \left( \frac{m_e}{m_p} \right)^2 0.665 \cdot 10^{-28} \text{ m}^2$$

We have to take into account for the phase lag of the individual electrons w.r.t. each other:

$$\sigma_{ud} = \sum_{i=1}^N \sigma_T \cos(kx)$$

$$k = \frac{2\pi}{\lambda_d} \quad x = |\vec{x}_1 - \vec{x}_i| + |\vec{x}_2 - \vec{x}_i|$$