

# Intrinsic variation in physics events for ORCA

ecap

ERLANGEN CENTRE  
FOR ASTROPARTICLE  
PHYSICS

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Thanks also to M. Pleinart, T. Rauch

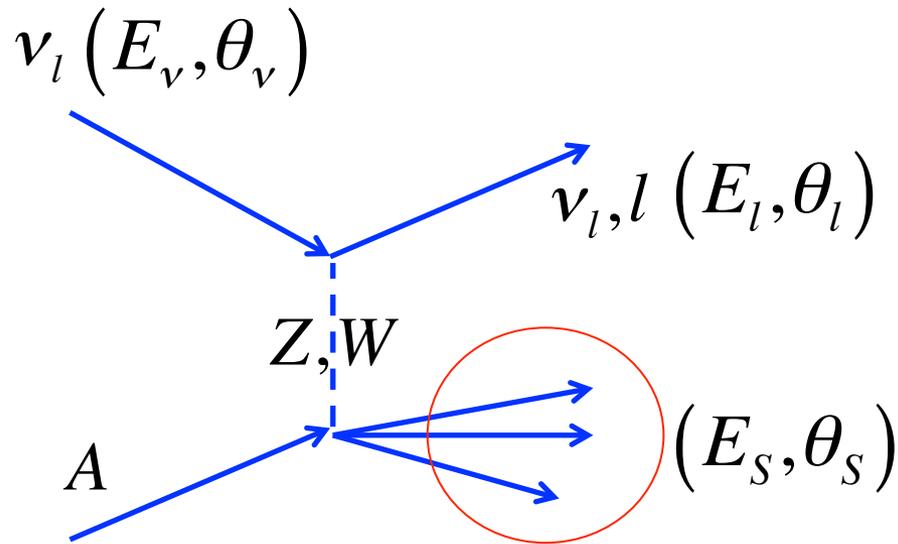
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# Detectors see showers and tracks via photons

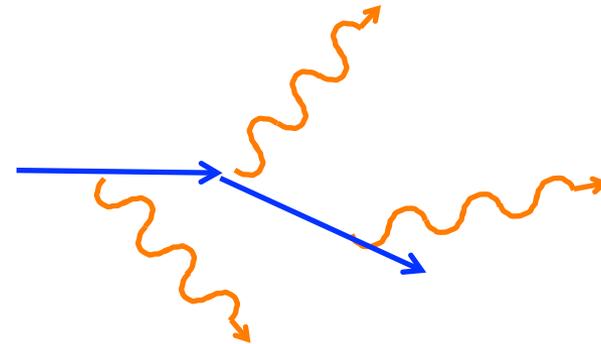


$$\vec{p}_v = \vec{p}_l + \vec{p}_s$$

$$E_v = E_l + E_s$$

## Information via photons:

- Number  $\sim$  energy
- Direct photons  $\sim$  direction



## Physical mechanism:

- Vertex physics
- Particle propagation
- Cherenkov emission

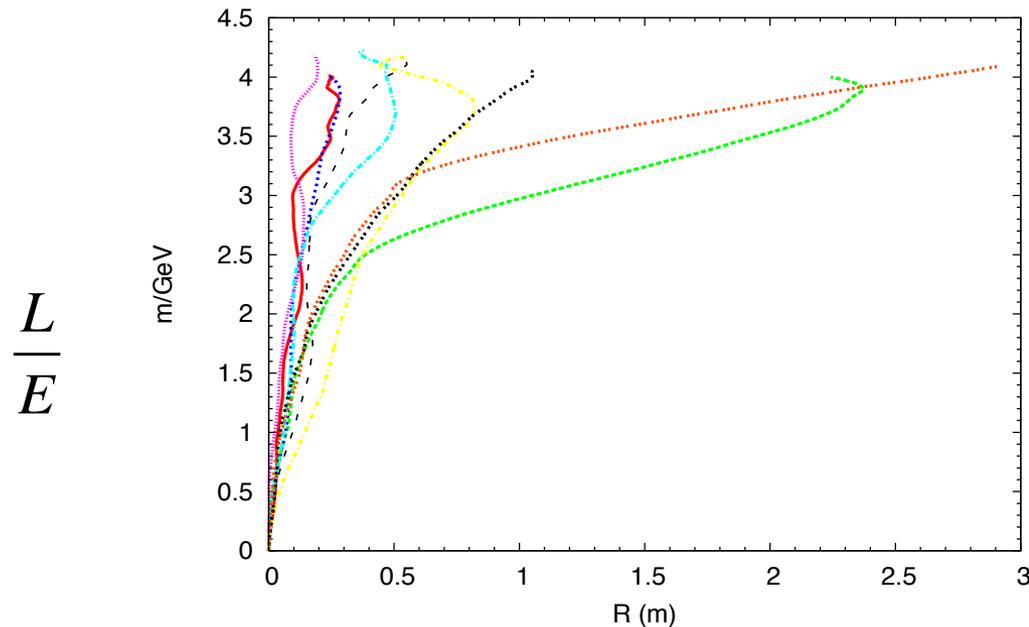
- What is the effect of intrinsic fluctuations in the physics?

# Principles

- What is the best we can do if we detect every single photon?
  - Simulate many identical events
  - Look at fluctuations in photon output and track behaviour
- Given we detect only some photons, what's the best we can do?
  - Estimate mean detector response
  - What minimum error does this give us?
  - Always make optimistic assumptions on detector response

# Muons: tracklength and deviation

- 10 Muon tracks, 3-13 GeV:

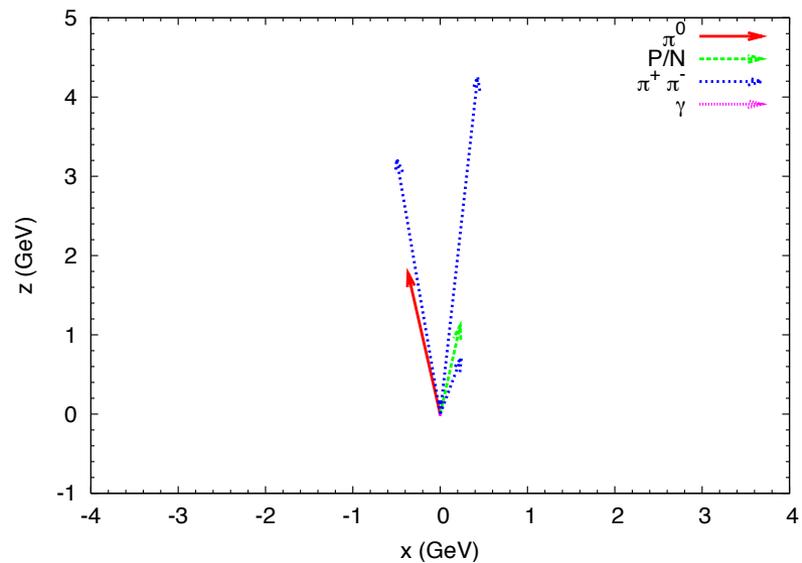
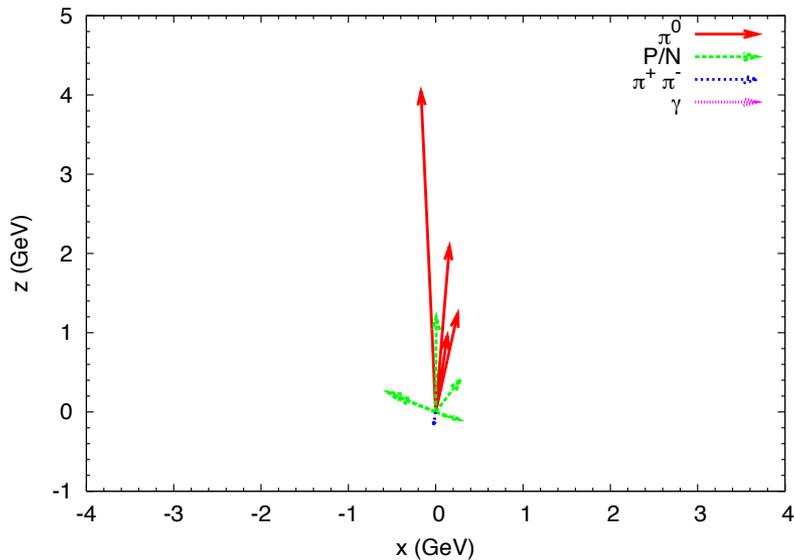


- They are not perfect straight lines (direction error)
- Length also differs (energy error)

# Showers: vertex effects

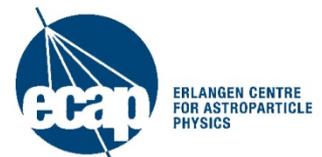
- 2 events: same momentum transfer at the vertex

Plot:  
 $E_{kin} \hat{V}$



- Additional source of variation:
  - Composition of the cascade
  - Energy/momentum of recoil nucleus

Pi0  
 Nucleons  
 Pi±  
 Gammas



# Principles

- Muons
  - Energy: estimate using true muon track length
  - Direction: use a linear fit to the track
- Showers:
  - Energy: estimate using total detected photons
  - Direction: mean photon direction – *using direct photons only.*
- Assumptions: always make optimistic ones!
  - Know where photons come from
  - Perfect vertex reconstruction
  - Do not model detector effects

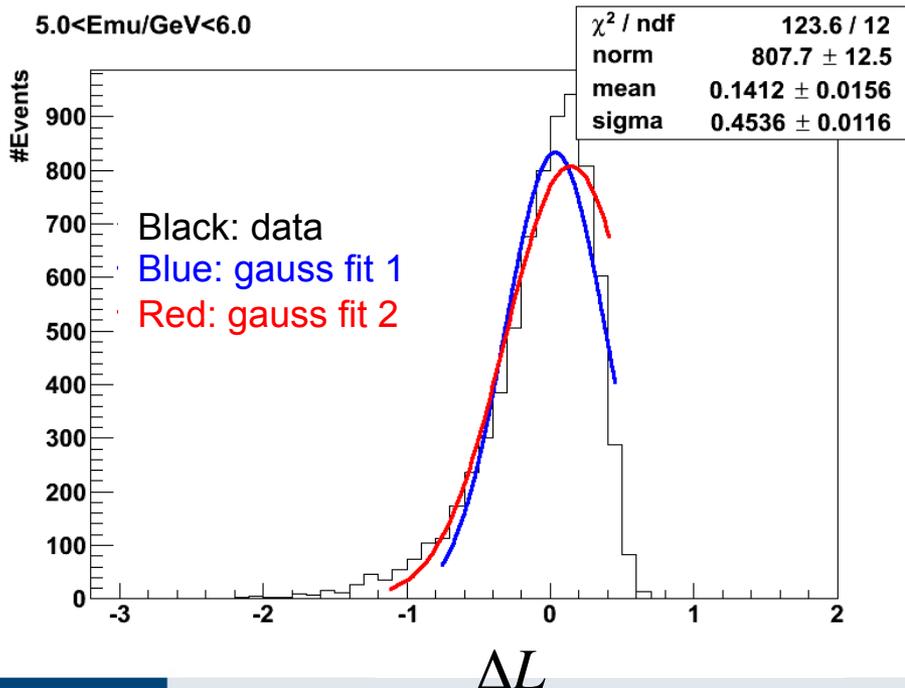
# MUON TRACK FLUCTUATIONS



# Muons: energy (method)

- Muon energy - estimate it through the tracklength
- ‘MUSIC’: muon tracking in km<sup>3</sup>
  - output muon track information for many events
- Run muons of a given energy, record tracklength

$$\frac{\Delta L}{L} \Leftrightarrow \frac{\Delta E}{E}$$

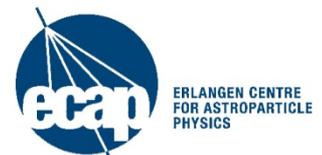


$$\Delta L = L - 4.25 \frac{E}{1 \text{ GeV}}$$

- Fit using gaussians: use
  - central peak (fit 1)
  - all data (fit 2)
  - Simple root mean square

8

Courtesy J. Hofestädt

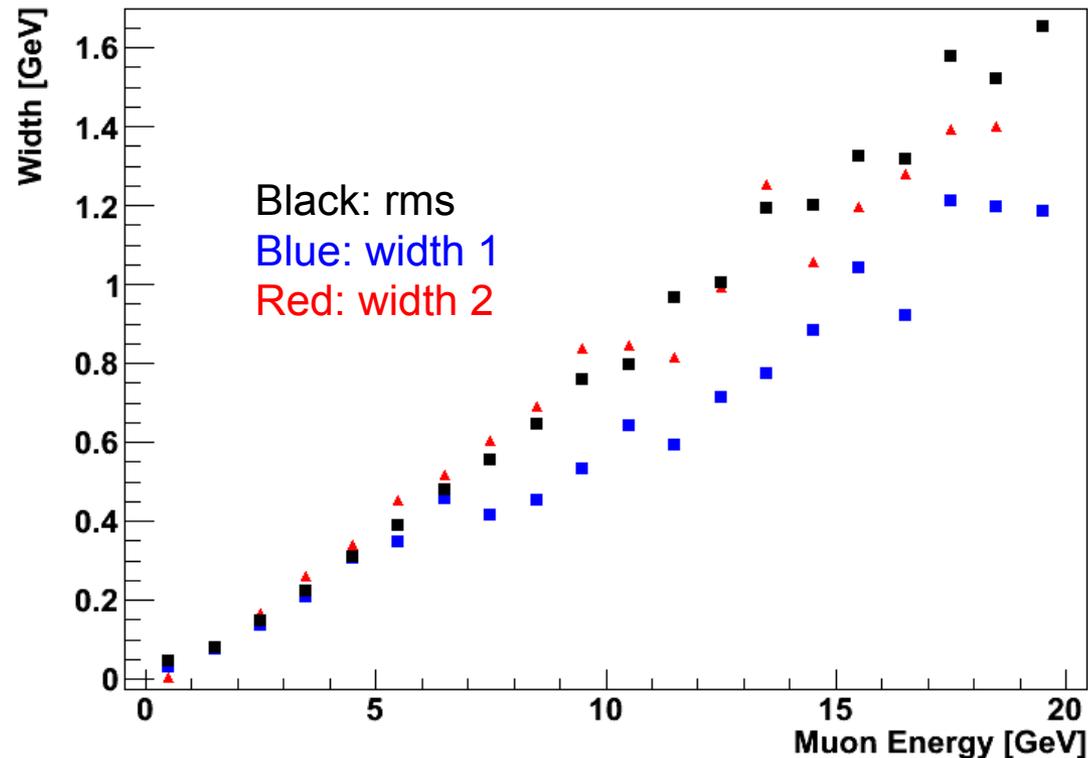




## Muons: energy (results)

- Intrinsic spread from physical fluctuations

$$\Delta E = \frac{\Delta L}{4.25 \text{ m}}$$

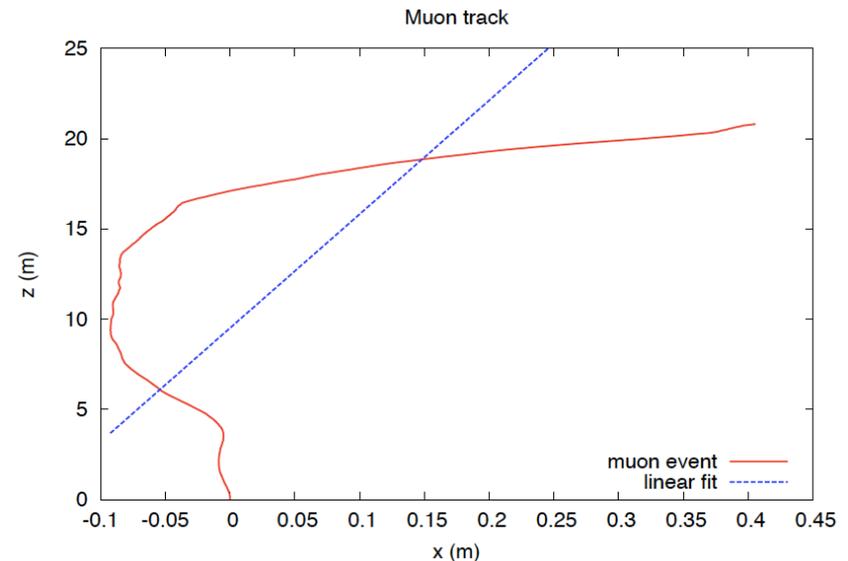
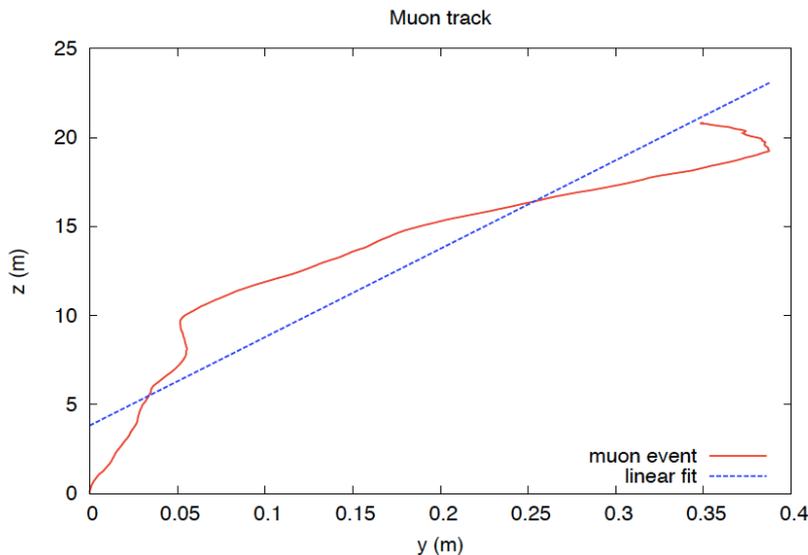


Courtesy J.  
Hofestädt

- Approximately 8% muon energy resolution

# Muons: direction (method)

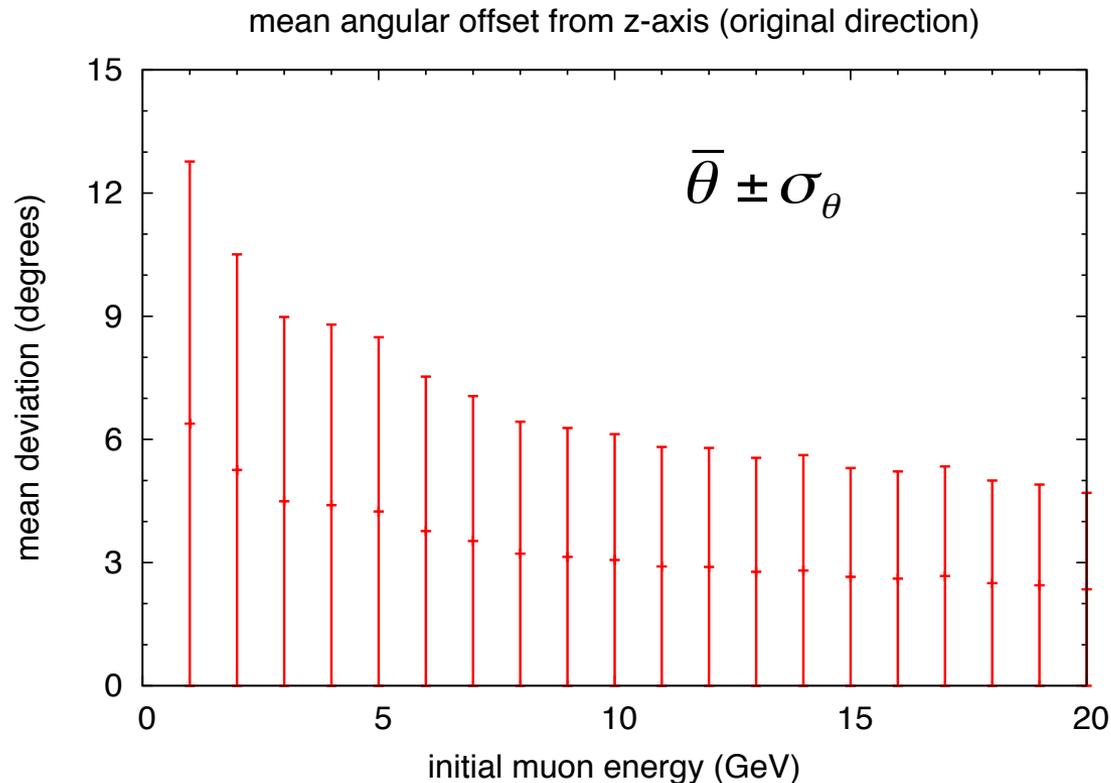
- How straight are muon tracks?
  - Run 2000 muons over 0-20 GeV range with GEANT 3.21
  - Get  $x(z)$  and  $y(z)$  with simple linear fit
  - Obtain angular offset  $\theta = \cos^{-1}(\hat{v}_{fit} \cdot \hat{z})$



Courtesy M. Pleinert

# Muons: direction (results)

- Estimation of intrinsic variation:



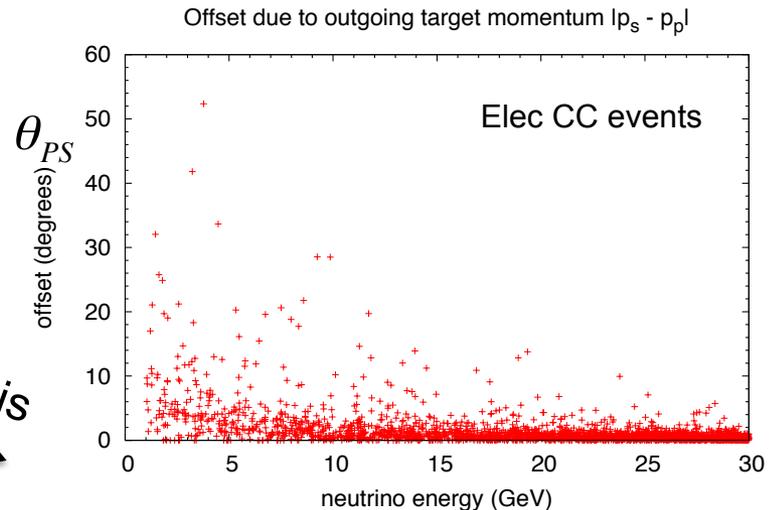
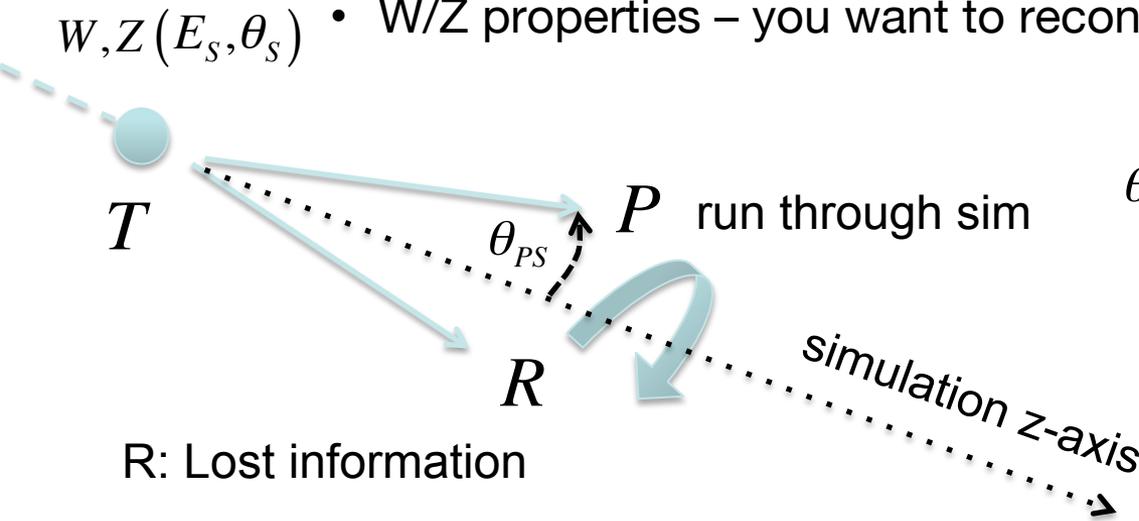
Courtesy  
M. Pleinert

- 10 GeV muons:  $\sim 4^\circ$  intrinsic error
- Work still needed to characterise this (true dist 2D)

# SHOWER FLUCTUATIONS

# Showers: definitions

- Outgoing particles:  $B + T \rightarrow R + P$ 
  - Boson (B) + target (T)  $\rightarrow$  remnant (R) + energetic particles (P)
  - Target T and remnant R invisible
  - W/Z properties – you want to reconstruct these!



- Define ‘shower’ energy/momentum via the W/Z properties

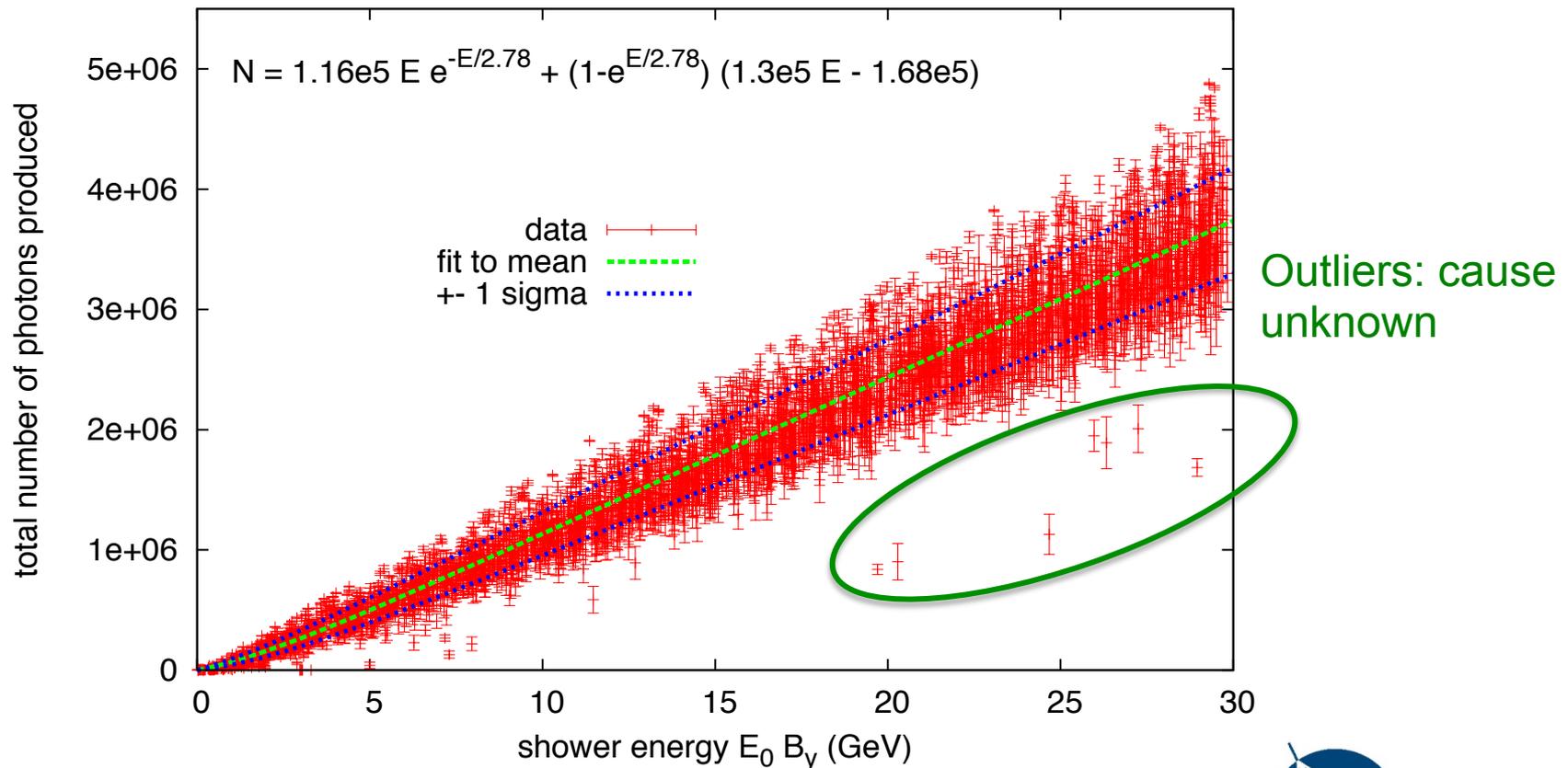
\*random target orientation and ~no coupling to e.g. magnetic moment of target

# Simulations

- Events from gSeaGen (12000)
  - 0-30 GeV range ( $E_s = yE_{\nu}$ )
  - 100 events per GeV (randomly selected)
  - 4 classes: NC/CC and Muon/Electron neutrinos
  - *Ignore leptons in CC events*
- Simulations
  - GEANT 3.21
  - Repeat 50 times for each of 12,000 events
  - Record photon statistics (number and direction)
- Analysis
  - Fit fluctuations within and between events
  - Energy error: total number of photons
  - Direction error: mean photon direction

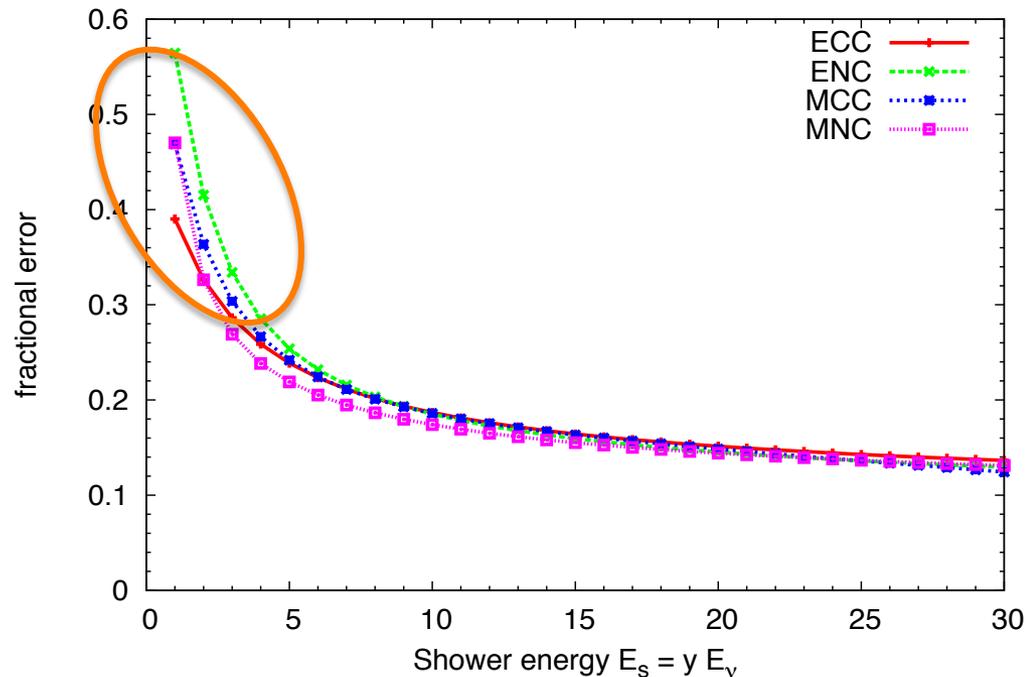
# Results: errors in energy resolution

- Each point: mean of 50 runs for each vertex
- Error bars: variation within these 50



# Total intrinsic variation: shower energy

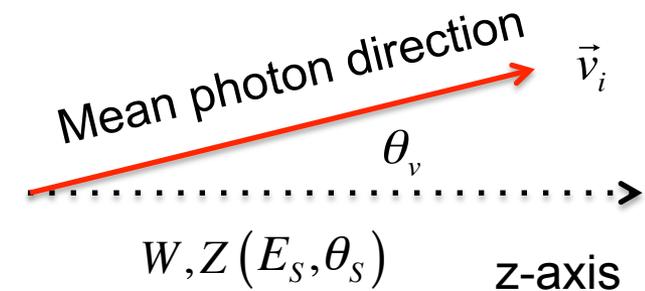
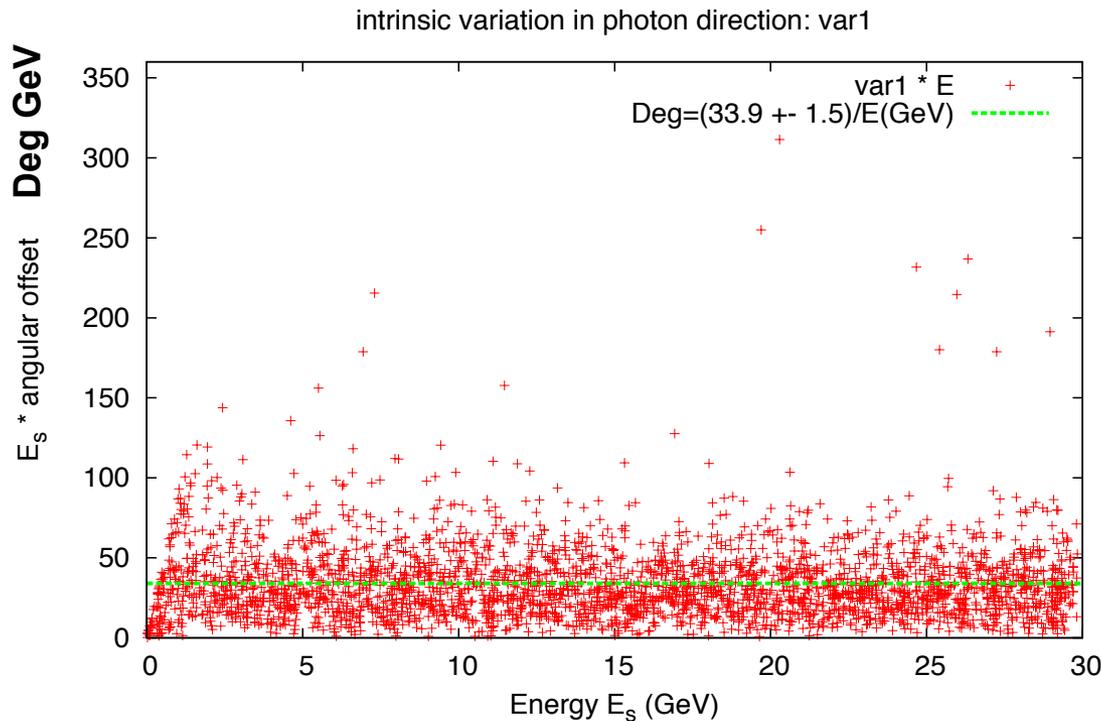
- Repeat for  $\nu_\mu$  and CC/NC events



- Fractional error in emitted photons  $\sim$  fractional error in energy reconstruction
  - 1 GeV showers:  $\sim$ 50% energy resolution
  - 10 GeV showers:  $\sim$ 20% energy resolution

# Results: direction ('vertex' variation $\theta_v$ )

- 1 point per vertex (mean over 50 runs)
- Plot offset of this mean from the z-axis

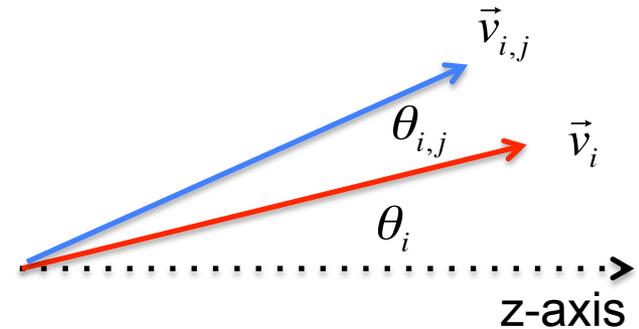
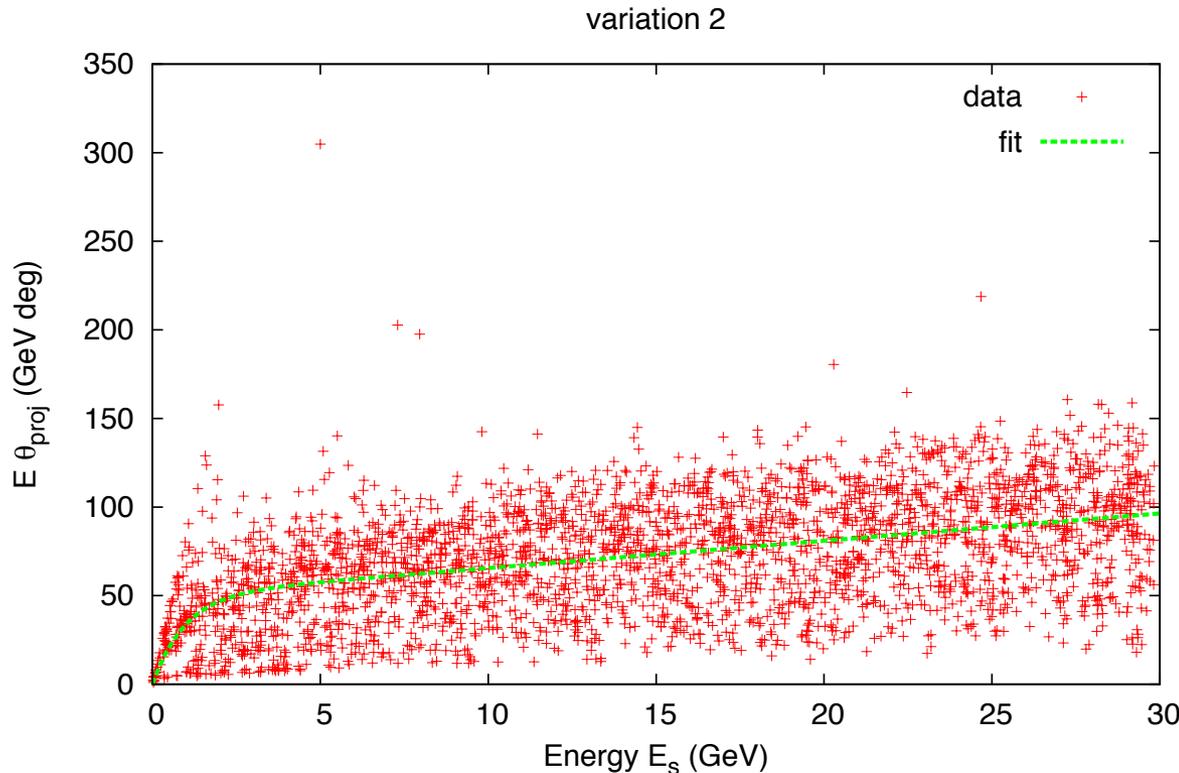


Mean direction  
over all 50 runs

- Fit: 34 degrees at 1 GeV, 3.4 degrees at 10 GeV

# Results: direction (cascade variation $\theta_c$ )

- Each point: variation of 50 runs about mean



Mean photon direction over all 50 runs

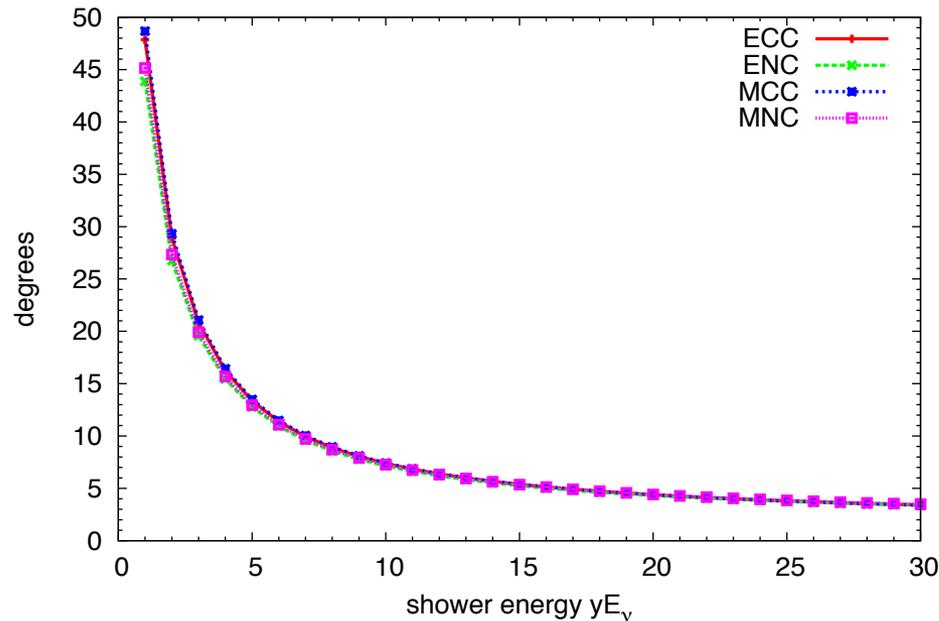
Mean photon direction for a single run

$$\theta_{i,j} \equiv \text{acos}(\vec{v}_{i,j} \cdot \vec{v}_i)$$

- 1 GeV: ~20 degrees
- 10 GeV: ~6 degrees

# Total intrinsic variation:

- Repeat for  $\nu_\mu$  and CC/NC events



Add errors in quadrature:

$$\theta_{tot} = \sqrt{\theta_1^2 + \theta_2^2}$$

- Fits statistically identical: no plans to repeat for anti-neutrino events.
- You will not be able to reconstruct showers better than this – even if you detect every single photon.

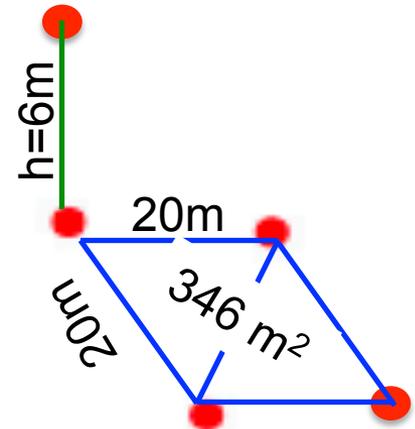
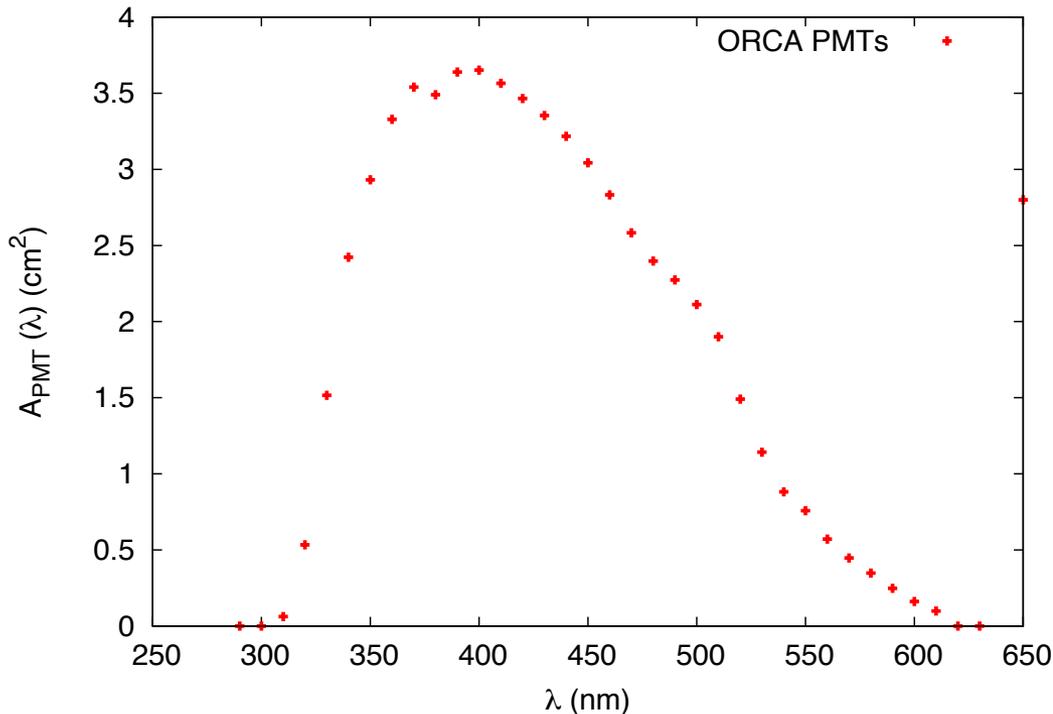
# DETECTOR LIMITATIONS

How are we limited by not detecting every photon?

# Detector Response

- What is the mean photocathode density in the ocean?

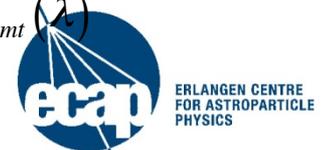
- Mean PMT effective area:  $\bar{A}_{PMT}(\lambda) = \frac{1}{4\pi} \int_0^{2\pi} A(\lambda, \theta) 2\pi \sin\theta \, d\theta$
- PMT density for contained events:



Vertical spacing  $h=6\text{m}$   
 Horizontal area  $A=346 \text{ m}^2$   
 1 OM per  $2076 \text{ m}^3$

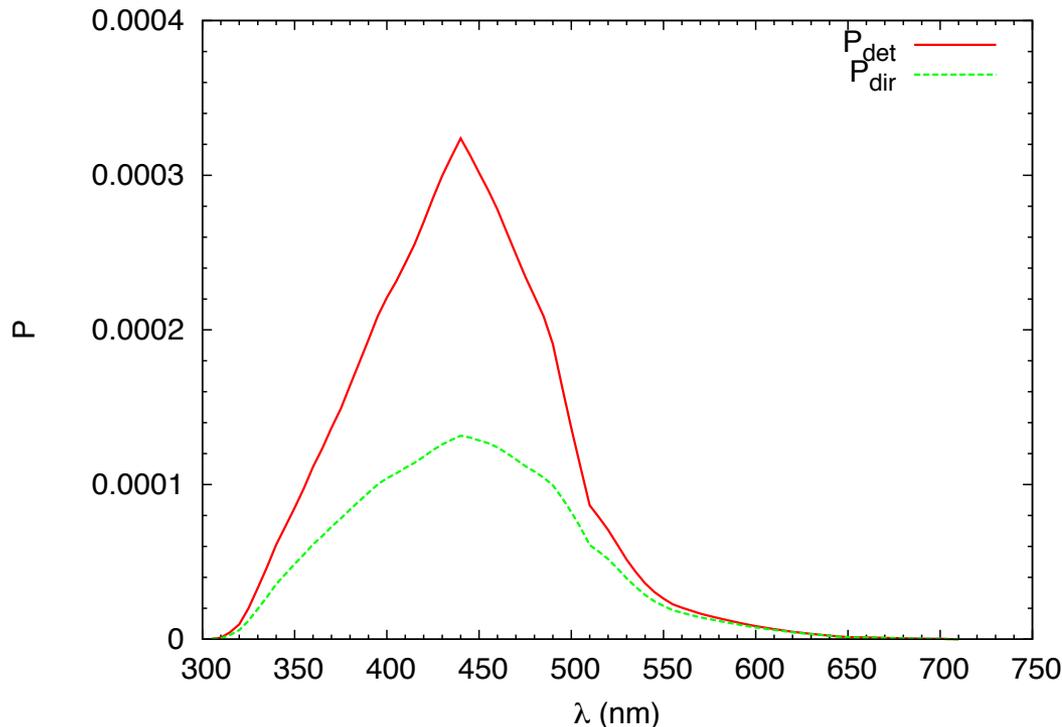
$$\rho_{pmt}(\lambda) = 0.015$$

$$l_{det}(\lambda) = \frac{1}{A_{pmt}(\lambda) \rho_{pmt}(\lambda)}$$



# Result: chance of detecting any given photon

- Probability of:
  - any detection (energy reco):
  - direct detection (direction reco):



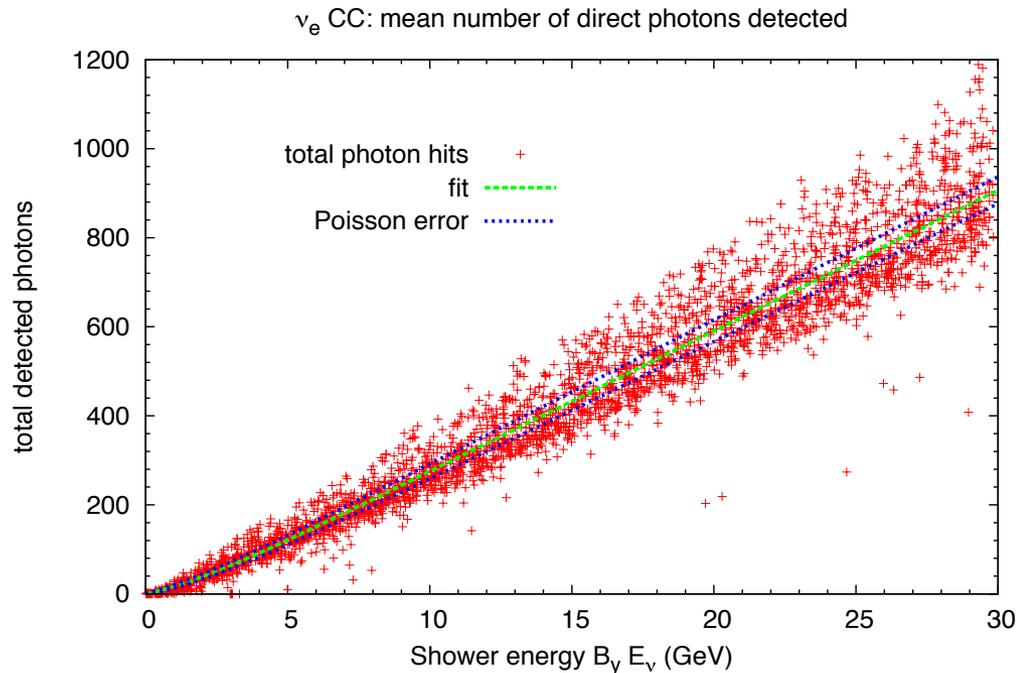
$$P_{\text{det}}(\lambda) = \frac{l_{\text{det}}(\lambda)}{l_{\text{abs}}(\lambda)}$$

$$P_{\text{dir}}(\lambda) = \frac{l_{\text{det}}(\lambda)}{l_{\text{att}}(\lambda)}$$

Expect half photons  
to be detected  
unscattered

# Detector energy uncertainty

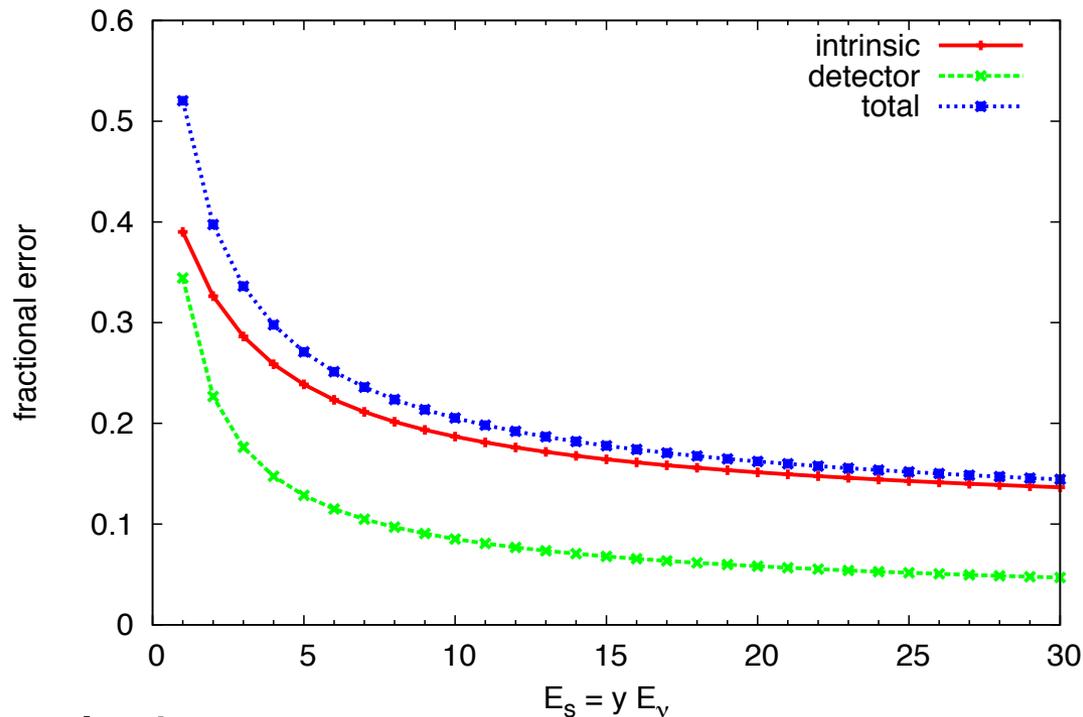
- How many shower photons get detected?



- Energy error  $\geq$  Poisson error  $\frac{\Delta E_{\text{det}}}{E} \sim N^{-0.5}$
- Assumes 100% identification of shower hits, ignores detector clumpiness,...

# Results – shower energy reco

- Comparison: **intrinsic**, **ORCA**, **total**

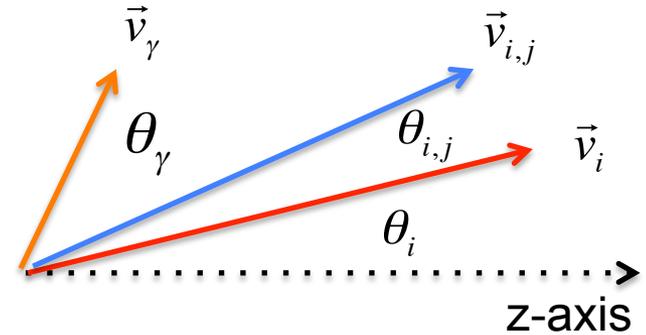


- Conclude:
  - Energy reco: intrinsically limited
  - Perhaps a sparser detector would be best?

# Detector limits: direction

$$\sigma_s = \frac{\sigma_\gamma}{\sqrt{N_{dir}}}$$

- Shower direction: average direction of all direct photons
- How well can we estimate the mean?



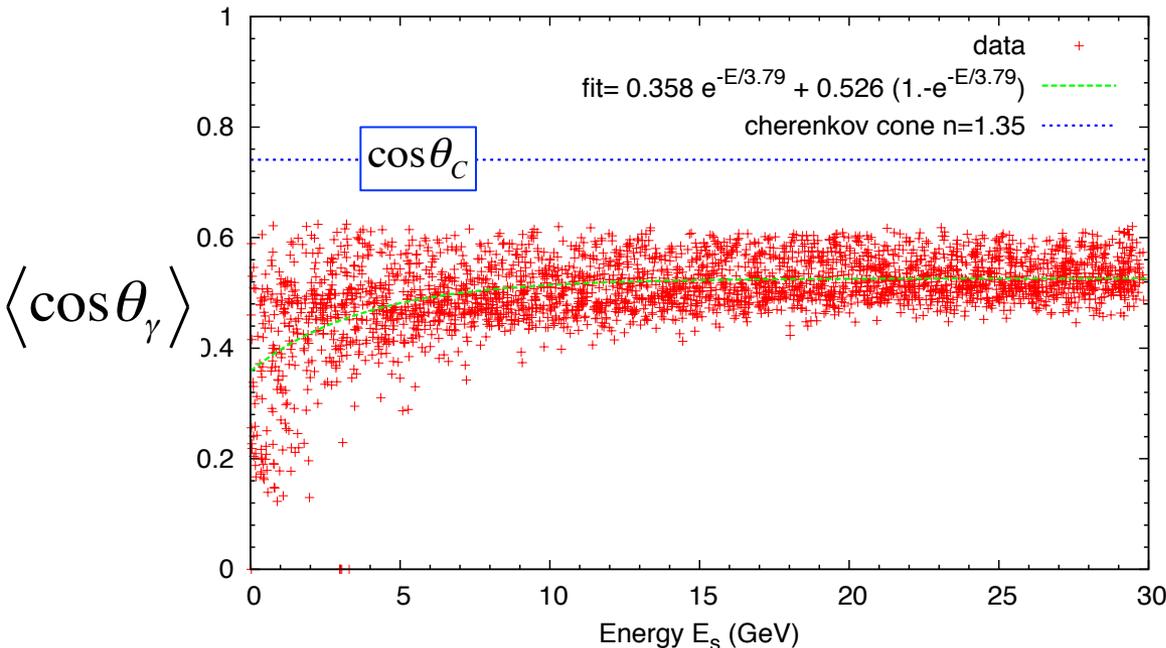
Mean photon direction over all 50 runs

Mean photon direction for a single run

Mean offset of each photon from the mean shower direction

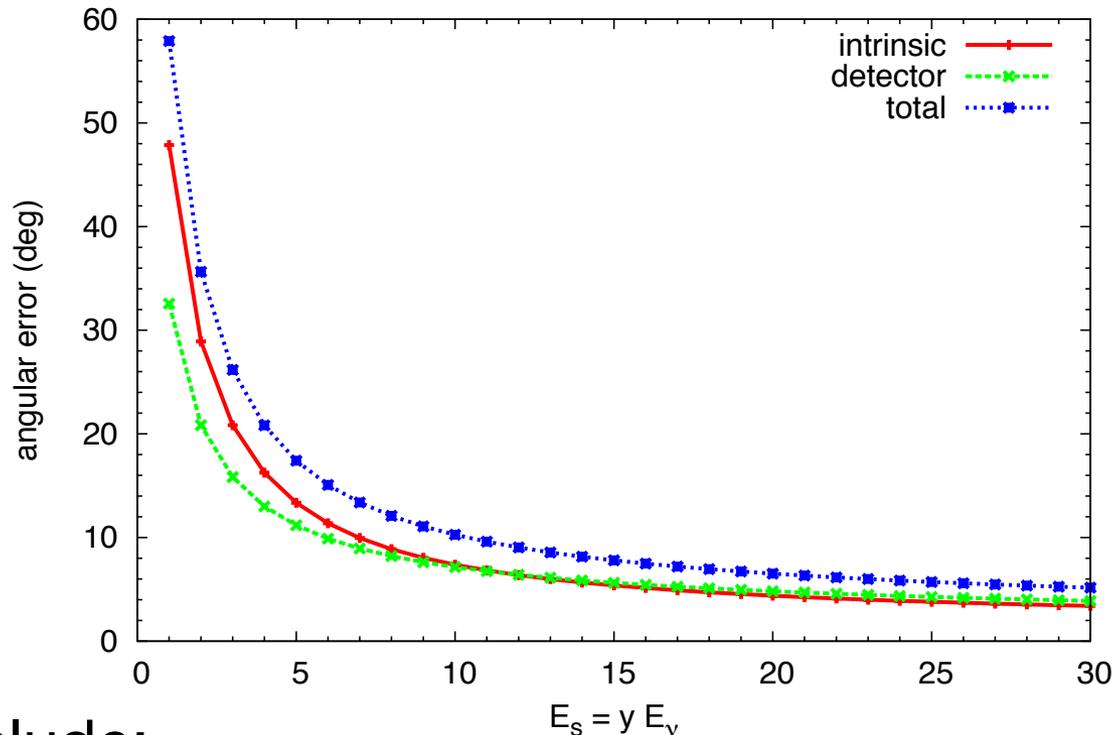
$\vec{v}_{sh}$

mean cosine between photons and shower direction



# Results – shower direction reco

- Comparison: **intrinsic**, **ORCA**, **total**



- Conclude:
  - Directional reco: detector effects significant
  - A denser detector would help

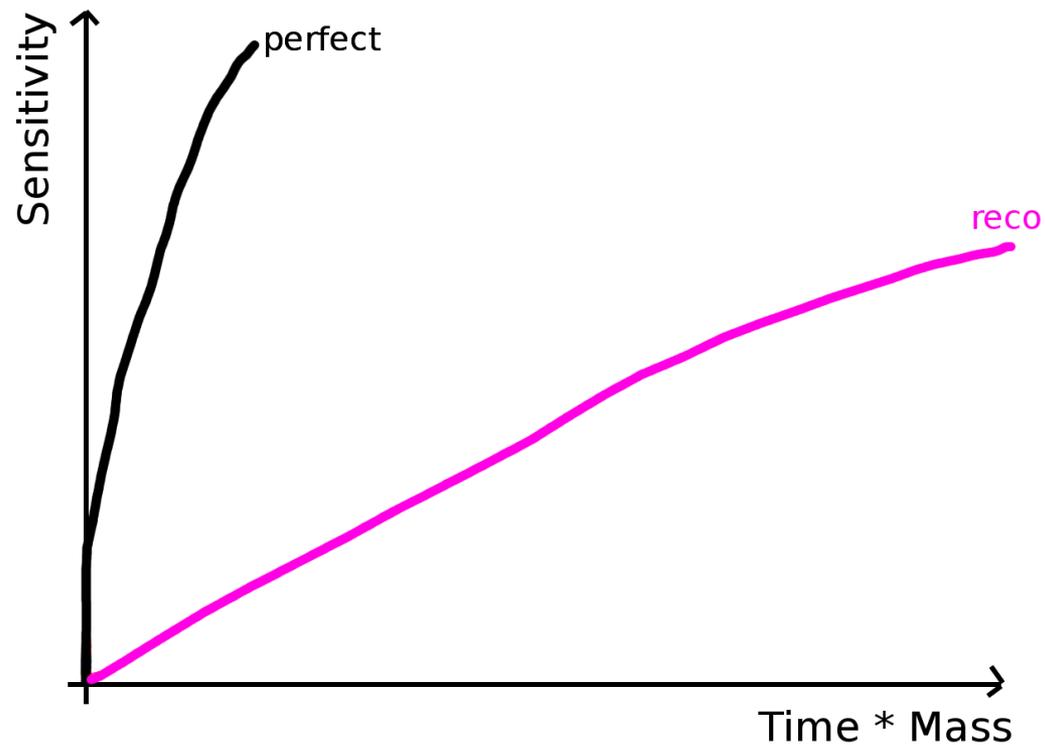
# What use is this?

- Compare to current reconstruction efforts
  - How close is your method to ‘perfect’?
- Use to influence detector design
  - Are we detector-limited or physics-limited?
- Determine limits to mass hierarchy sensitivities



## Incorporation into sensitivity plots:

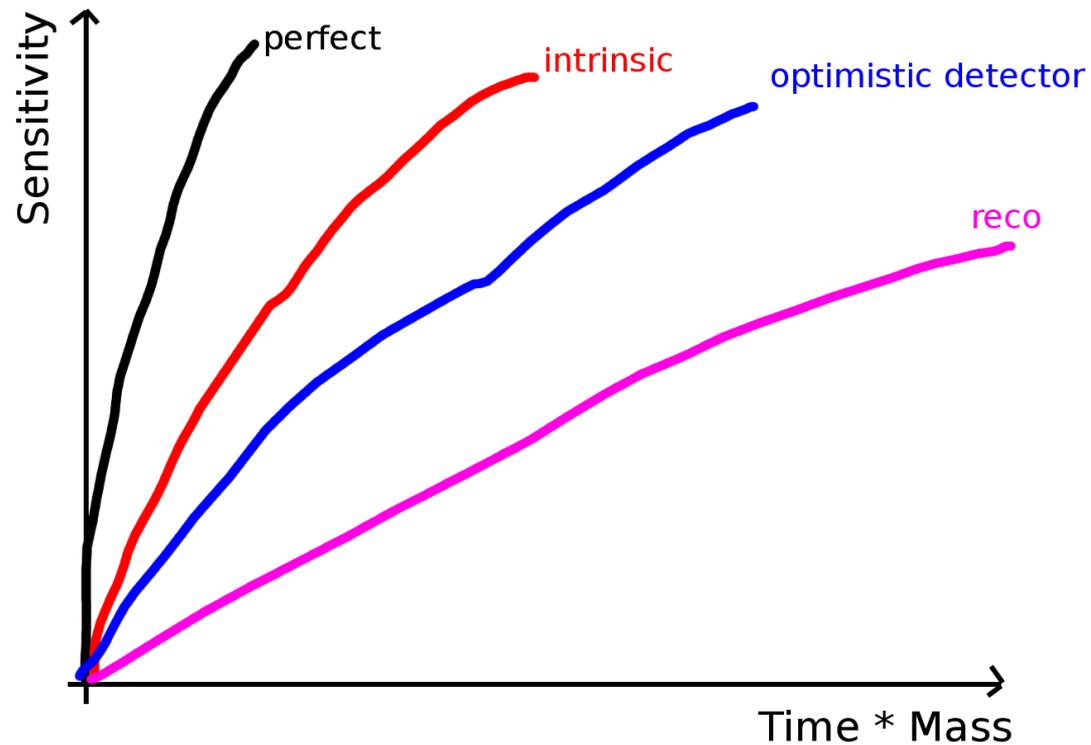
- Current situation:





## Incorporation into sensitivity plots:

- Sketch of the future:



# Summary of status

- Physics is random – and this is important!
  - Affects energy and directional reconstruction
  - Effects estimated for muon tracks and showers
- Best-case ORCA reference detector estimated
  - Event reconstruction will be limited by detected photon information
- Next steps:
  - Do this for electromagnetic cascades (Nu\_e CC)
  - Obtain fits for muon track events
  - Produce sensitivity estimates