

Honda flux

Sato (Nagoya U.)

14, Sep., 2019 @ Diffuse Workshop on Global Fit

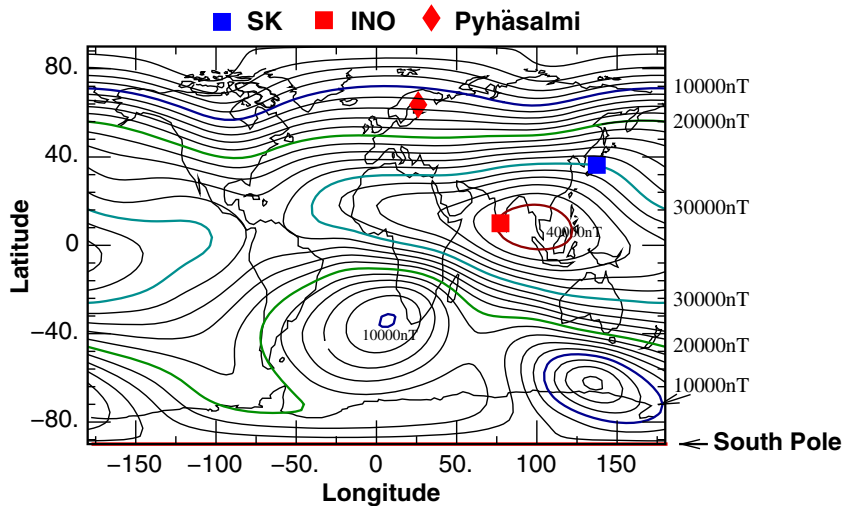
contents

- ATMNC : atm. v flux calculation code
- attempt to handle had. int. uncertainty by Nagoya group
- ongoing status

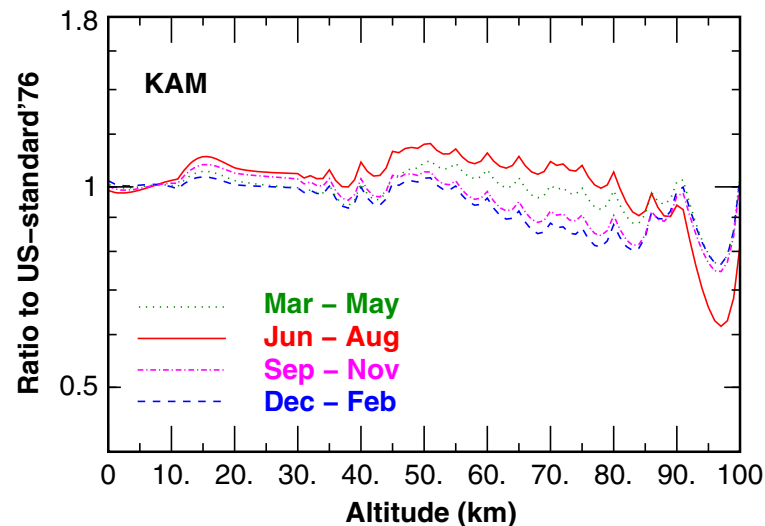
Honda's ATMNC

ATMNC: **ATM**ospheric **Muon** **N**eutrino **C**alculation code
developed by M. Honda (U of Tokyo, ICRR)
[PRD 83, 123001(2011) and references in it]

- used in Super-Kamiokande atm. ν analysis
- Full & 3D simulation
- several ideas for high speed computation



geomagnetic field based on
IGRF model

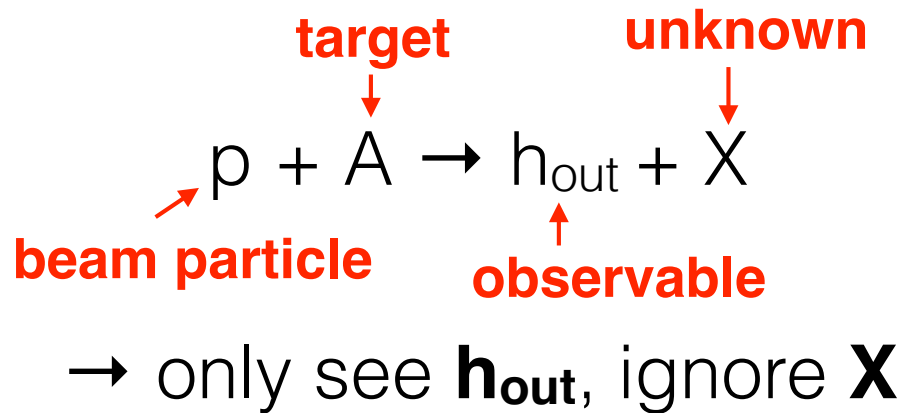


air density profile based on **NRLMSISE-00**
• for each month to handle seasonal
variation

hadronic interaction in ATMNC

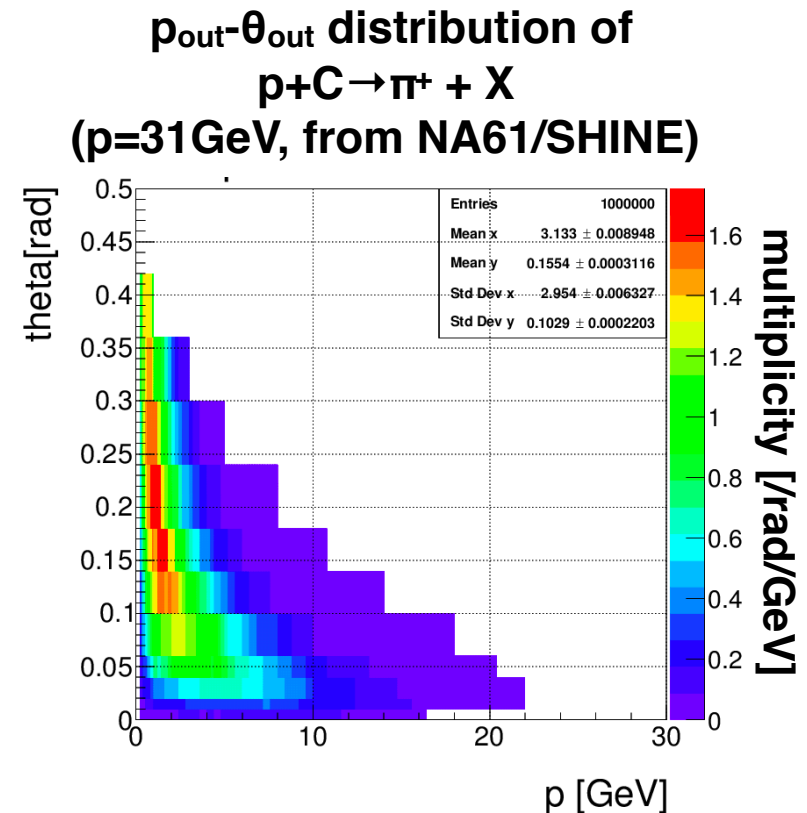
ATMNC adopts ***inclusive*** code for speed-up

Beam experiment for hadronic interaction measurement is usually *inclusive*



what they measure

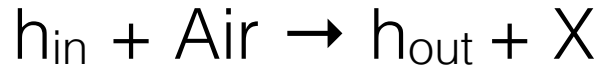
- multiplicity **$n(\mathbf{p}_{\text{in}})$** of h_{out}
- **\mathbf{p}_{out}** distribution of h_{out}
- **θ_{out}** distribution of h_{out}



Hadronic interaction in ATMNC is also *inclusive*

cont.

ignore



($h_{out} : \pi^{+,-,0}, K^{+,-,0}, p, n, \bar{p}, \bar{n}$)

ex) π^+ production from $p + A$

- 1) generate $N_{\pi^+}(p_{in})$ π^+ s
- 2) p_{out} of each π^+ are randomly sampled from E_{out}/E_{in} distribution
- 3) projectile angle of the π^+ is also sampled from $\cos\theta$ distribution

... also the same for other particles

- not correct for single CR event

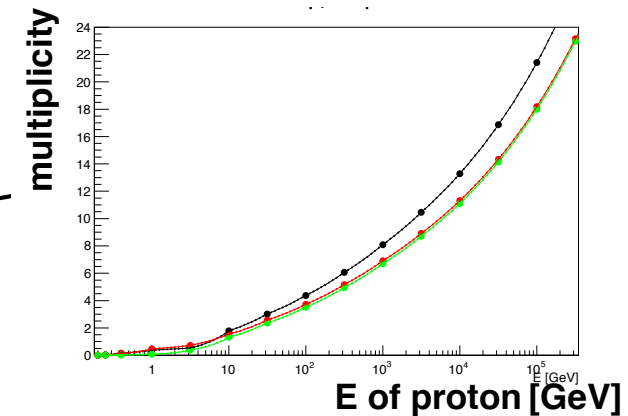
→ by **accumulating statistics**, **correct flux** is reproduced

pre-simulated tables

$N(E_{in}), E_{out}(E_{in}), \theta(E_{in}, E_{out})$

multiplicity (N_{π^+})

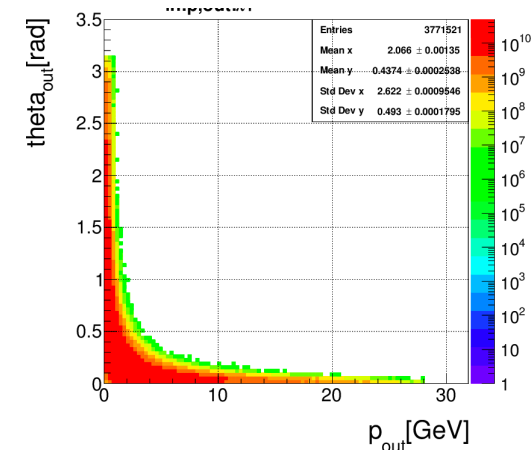
for $p+\text{air} \rightarrow \pi^{+,-,0} + X$



$p_{out}-\theta_{out}$

for $p+\text{air} \rightarrow \pi^+ + X$

(visualize as 2D hist.)



- made from event generator
 - JAM** ($E_{inc} < E_{JAM} = 31.6 \text{ GeV}$)
K. Niita et al., Radiat. Meas. 41, 1080 (2006)
 - dpmjet3** ($E_{inc} > E_{JAM}$)

multiplicity table, E_{out}/E_{in} table

for **every combination of $h_{in} \times h_{out}$**

- $h = p, n, \pi^+, \pi^-, 0, K^+, K^-, 0 + (e, \gamma \text{ for JAM } h_{out})$

for **each E_{in}**

- 25 division from $0.1 \text{ GeV} - E_{JAM}$
- 10 division from $E_{JAM} - 10^3 \text{ TeV}$
 - equal space in log scale

$\cos\theta_{out}$ table

for **every combination of $h_{in} \times h_{out}$**

- $h = p, n, \pi^+, \pi^-, 0, K^+, K^-, 0 + (e, \gamma \text{ for JAM } h_{out})$

for **each $E_{in} \& E_{out}$**

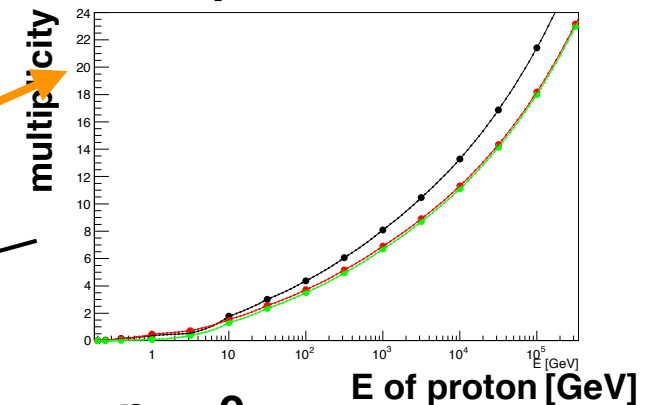
- 13 division for E_{in}
- 40 division for E_{out}
 - equal space in log scale

to inclusive

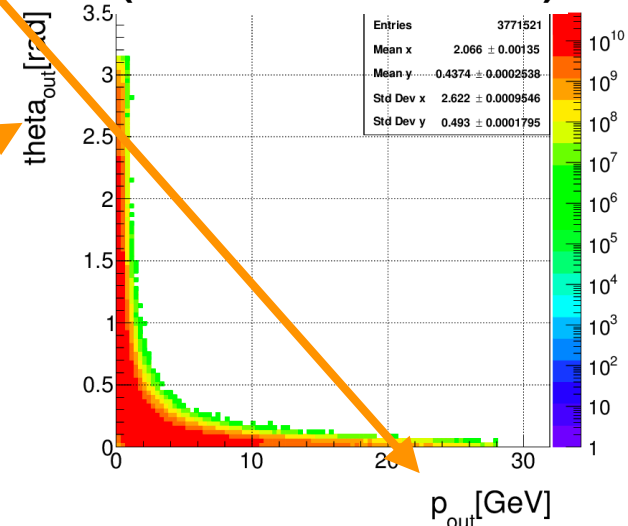
cont.

pre-simulated tables

**multiplicity (N_{π^+})
for $p+air \rightarrow \pi^+ + X$**



**$p_{out}-\theta_{out}$
for $p+air \rightarrow \pi^+ + X$
(visualize as 2D hist.)**

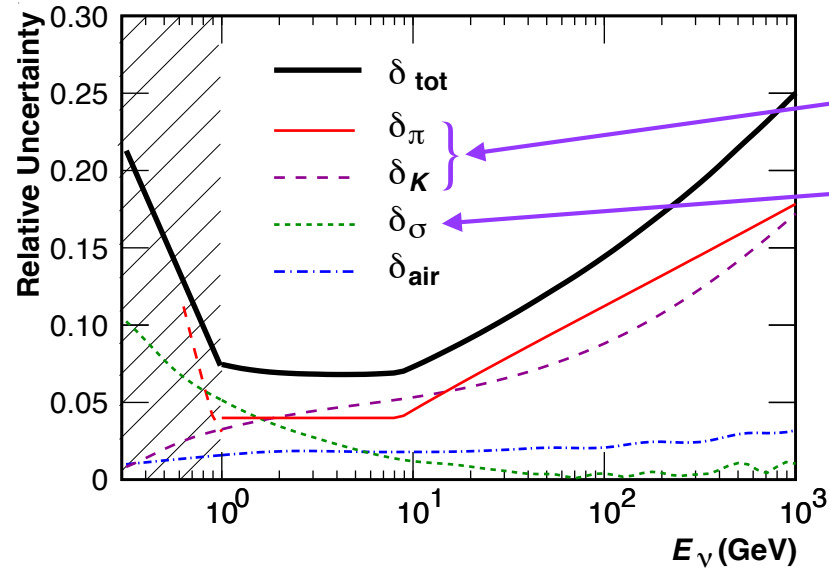


ect flux is reproduced

uncertainty of ATMNC flux

uncertainty of ATMNC flux

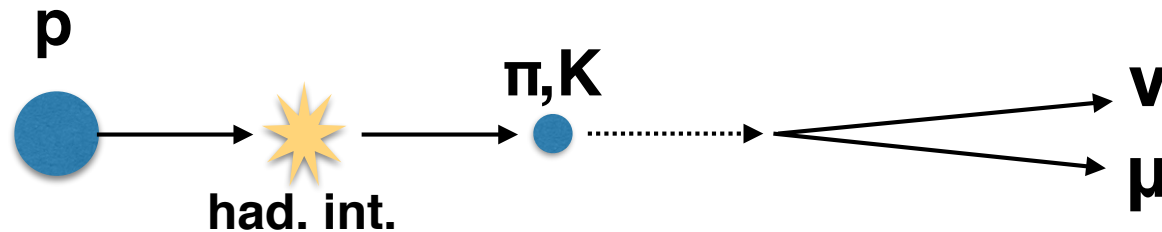
[M. Honda et. al, PRD75, 043006(2007)]



dominant uncertainty of ATMNC comes from the **uncertainty of hadronic interaction**

hadron interaction uncertainty

- Honda-san's study using cosmic-ray muon flux



μ & ν are produced in the same mechanism

→ response of μ flux to the change of hadron interaction strongly correlated to response of ν flux

$$\frac{\Delta\phi_{\mu}}{\phi_{\mu}} \simeq \frac{\Delta\phi_{\nu_{\mu}}}{\phi_{\nu_{\mu}}} \simeq \frac{\Delta\phi_{\nu_e}}{\phi_{\nu_e}}$$

Unfortunately, μ correlated to $<1\text{GeV}$ ν has too low energy to observe at ground level

→ large uncertainty in $<1\text{ GeV}$

*In TAUP2019 Honda-san shows the possibility that μ at $\sim 4500\text{ m}$ altitude covers the phase space of low-E ν
[[arXiv:1908.08765](https://arxiv.org/abs/1908.08765) (astro-ph.HE)]

activity of Nagoya group

to reduce the uncertainty

Nagoya group

Y. Itow

H. Menjo

K. Sato

start the study to incorporate the **hadron production measurement by beam experiment** into ATMNC directly

- Since this April

several measurement are conducted/planned
(mainly for **long-baseline ν experiment**)

HARP, BNL, NA61/SHINE, EMPHATIC ...

→ reflect these measurement by **referring the method used in T2K**

to reduce the uncertainty

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→ reflect these measurement by **referring the method used in T2K**

Maybe the measurement data is insufficient but...

- will **complement the phase space** where **Honda-san's muon study** does not covered
- can reveal **which phase space is important for atm. ν simulation**, and **feed back to the future beam experiment**

to reduce the uncertainty

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a common treatment of sys. error of hadronic interaction

→ **can discuss correlation of sys. error between T2K and SK, HK**

Maybe the measurement data is insufficient but...

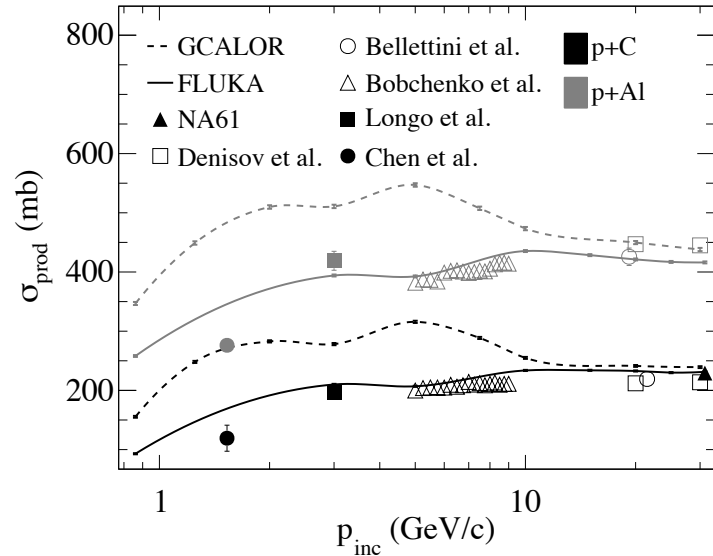
- **will complement the phase space where Honda-san's muon study does not covered**
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weighting method in T2K

They correct their MC by applying weight. [ref: PRD 87, 012001 (2013)]

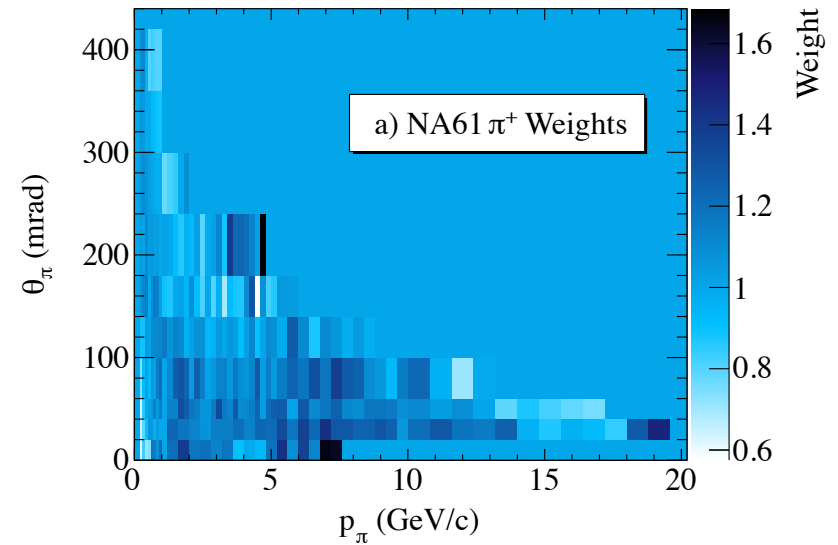
[from the T2K paper]

had.-production cross-section of p + C,Al



[from the T2K paper]

weight for p + C → π⁺ + X



atom density flight length

$$P = \exp(-\sigma \rho L) \times \sigma_{prod} \rho \Delta L$$

$$W = \frac{P_{Data}}{P_{MC}} = \frac{\sigma_{Data}}{\sigma_{MC}} \exp\{-L\rho(\sigma_{Data} - \sigma_{MC})\}$$

multiplicity at (p_{out}, θ_{out}) [1/GeV/rad]

$$W = \frac{\left(\frac{dn}{dpd\theta}\right)_{Data}}{\left(\frac{dn}{dpd\theta}\right)_{MC}}$$

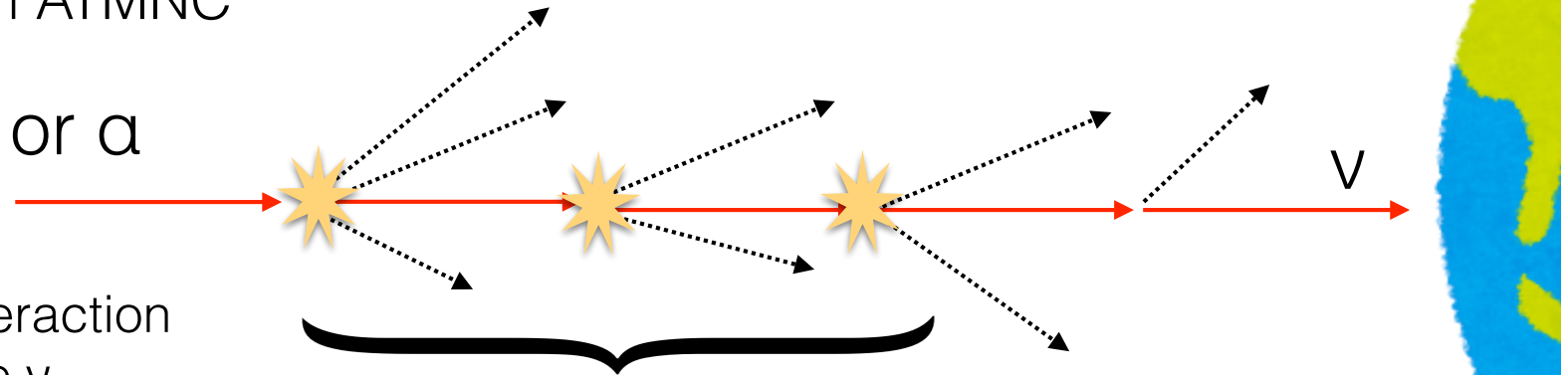
requirement for beam measurement

check what beam measurement is needed for atm. ν production

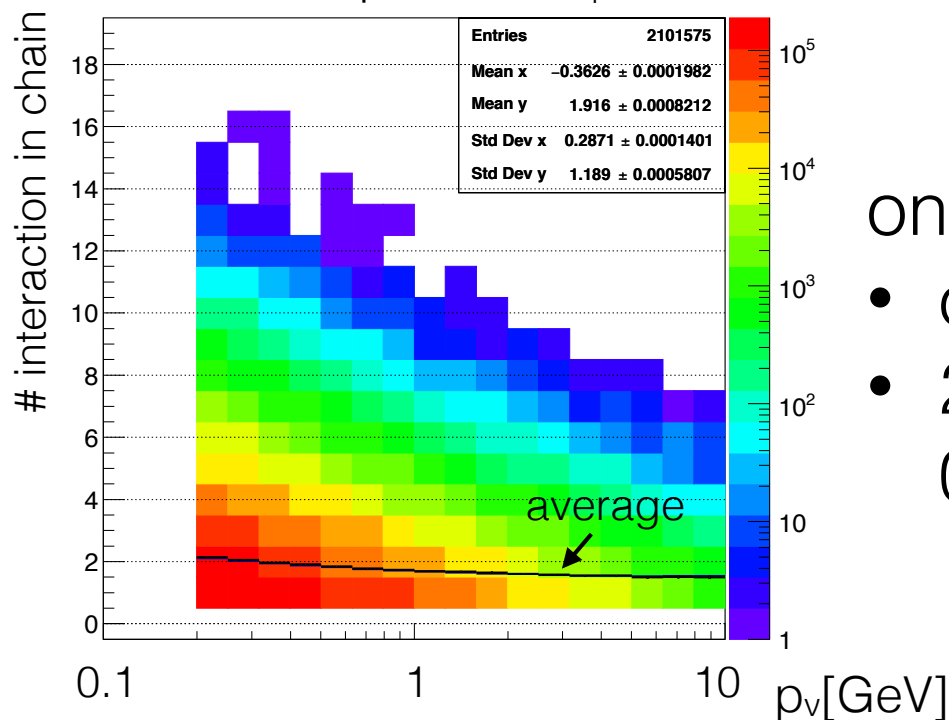
- beamE?
- kind of beam particle (h_{in}) and observable particle (h_{out})?

simulation with ATMNC

p or a



of hadron interaction
to produce ν_μ



How many hadron interactions?

only a few between the 1ry and ν

- of course 1ry interact once
- 2nd, 3rd, ... hadrons also induce 0.5-1.2 times interaction

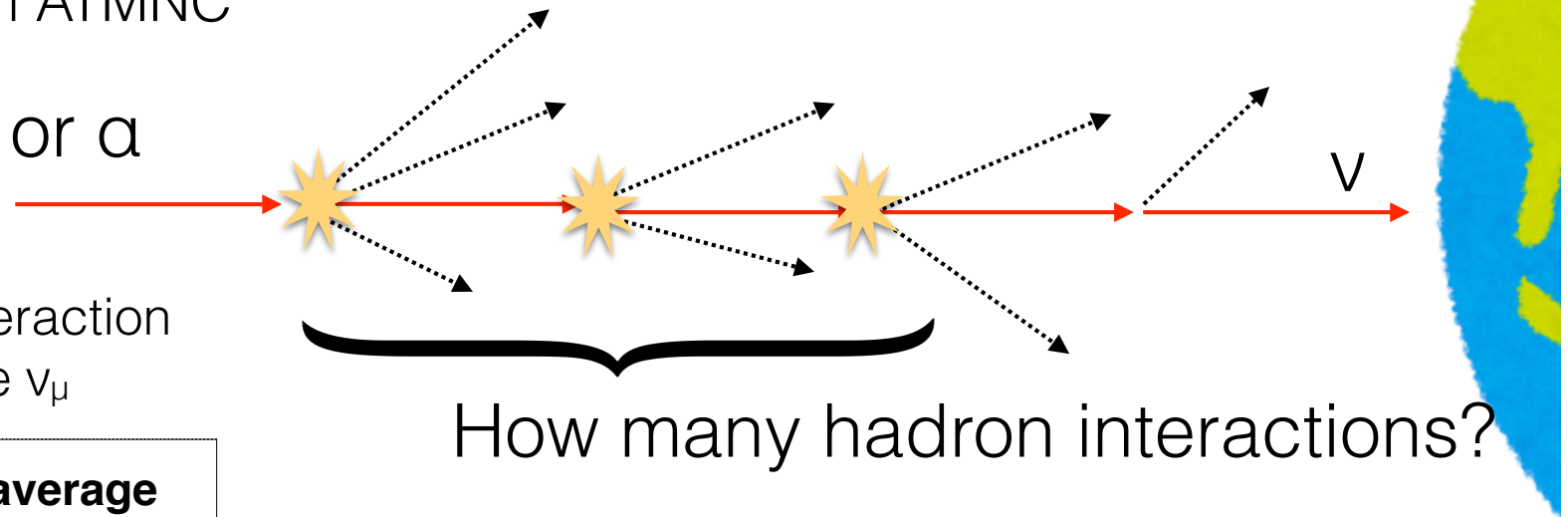
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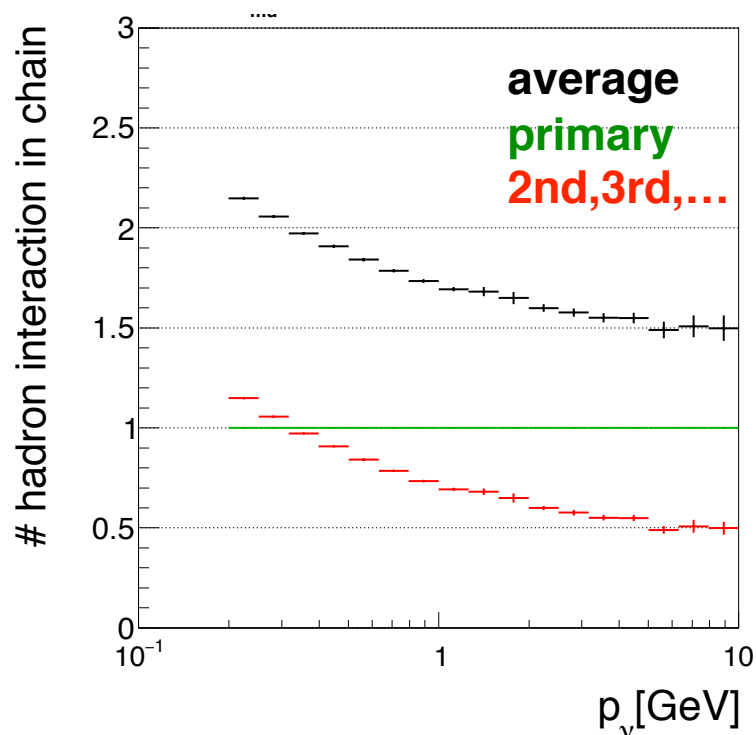
- kind of beam particle (h_{in}) and observable particle (h_{out})?
- beam E ?

simulation with ATMNC

p or α



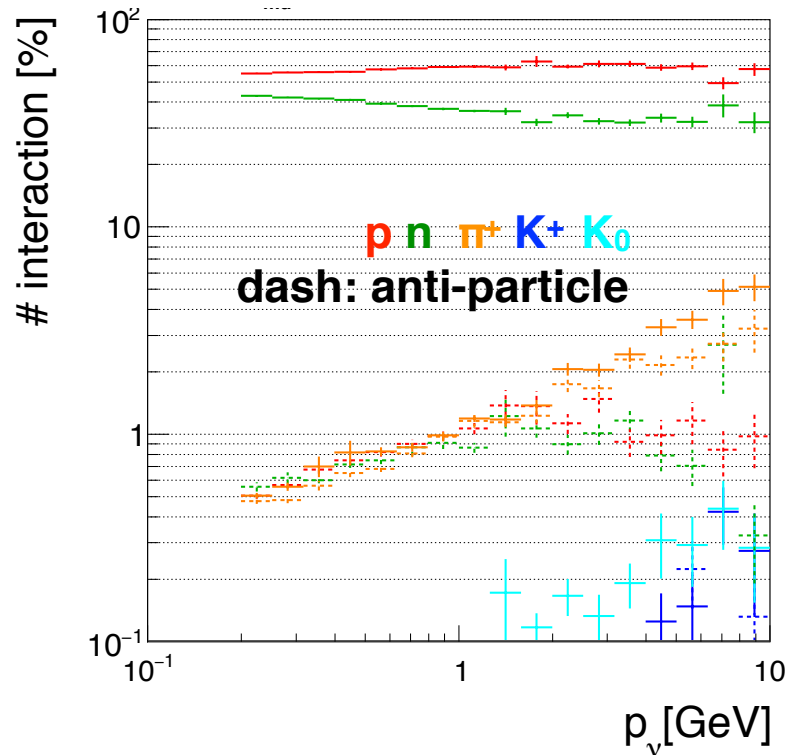
of hadron interaction
to produce ν_μ



- only a few between the 1ry and ν
- of course 1ry interact once
- 2nd, 3rd, ... hadrons also induce 0.5-1.2 times interaction

cont.

particle type of 2,3,...-th hadron
causing hadronic interaction



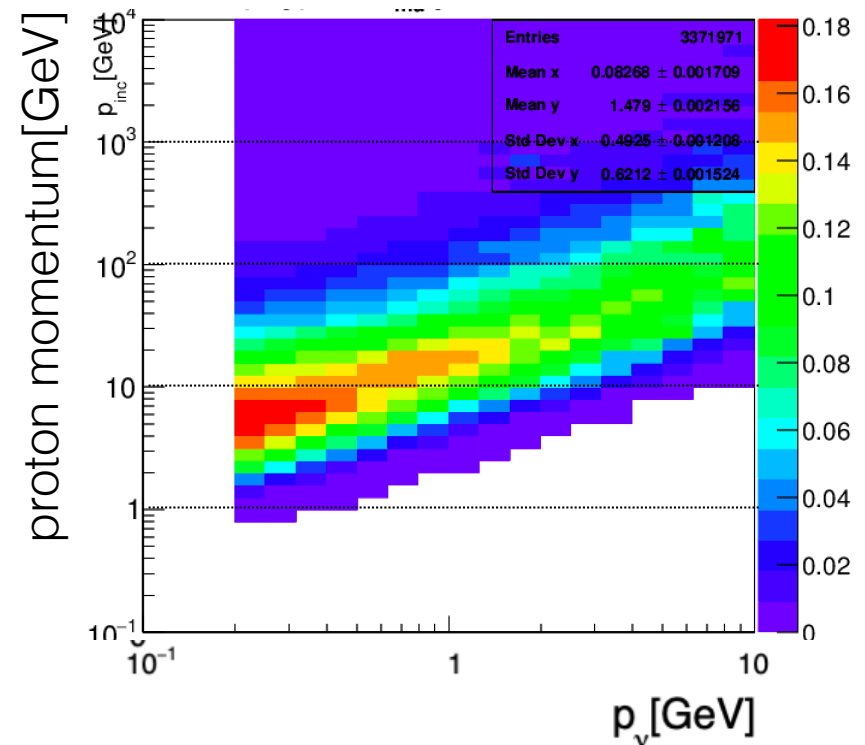
In sub- or multi- GeV region,
p,n is dominant

beam particle : p

peak of the incident p & n momentum
ranges 5—100 GeV

beam energy : ~5—100 GeV

incident p,n momentum involved
in hadron interaction in ν_μ chain



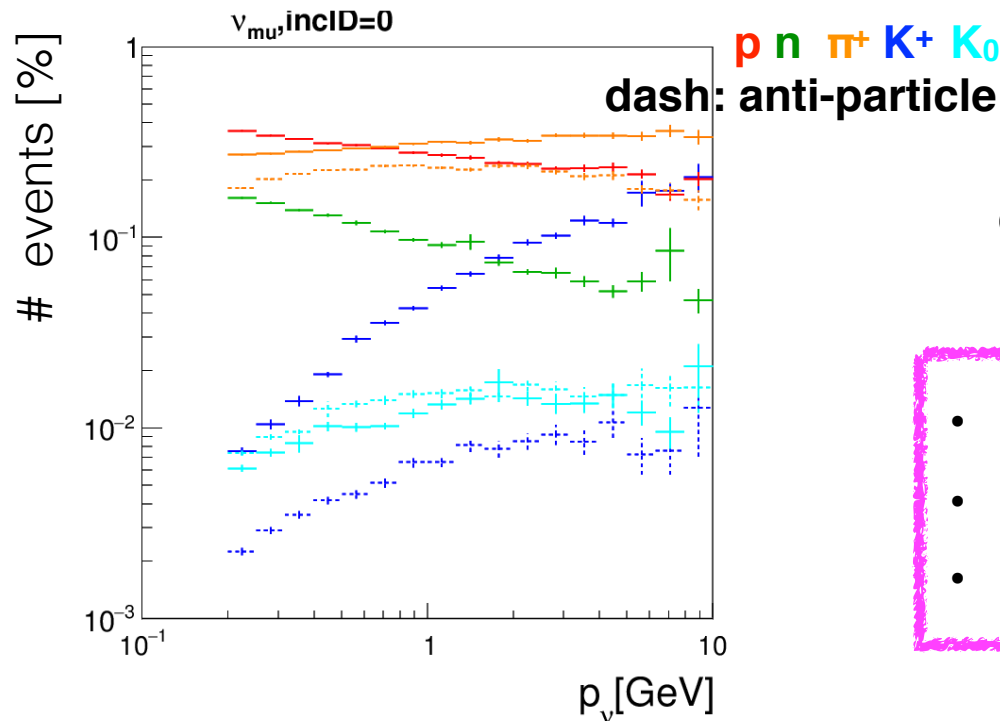
suitable beam measurement

particle emitted from hadron
interaction in ν_μ chain
(incident particle: proton)

kind of emitted particle

- π^{\pm}, p, n
- K^{\pm} also contributes

observed particle : π^{\pm}, K^{\pm}, p

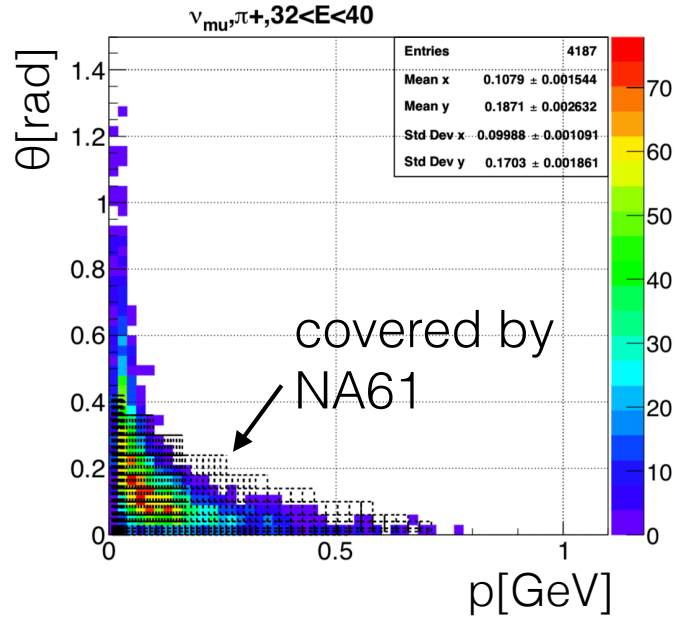


- **beam particle: p**
- **observed particle: p, π , K**
- **beam energy: $\sim 5 - 100$ GeV**

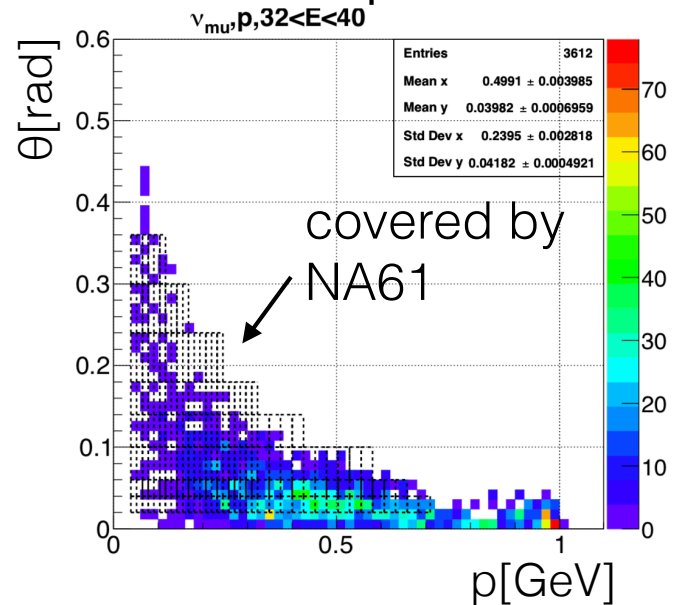
	target	beam P [GeV]	h_{out}	ref.
HARP	Be	8.9	π^+	Eur. Phys. J. C52(2007)
HARP	C	12	π^+, π^-	Astr. Phys. 29 (2008) 257
NA61/SHINE	C	31	p, π^{\pm}, K^{\pm}	Eur. Phys. J. C76 (2016)
BNL	Be	6.4, 12.3, 17.5	π^+, π^-	PRC77 015209 (2008)

$32 < p_{in} < 40 \text{ GeV}$

$h_{out} = \pi^+$



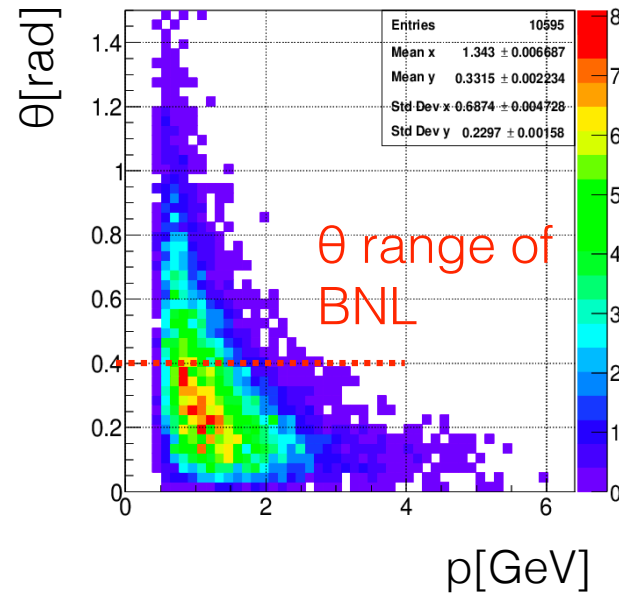
$h_{out} = \text{proton}$



Does measurement cover phase space?

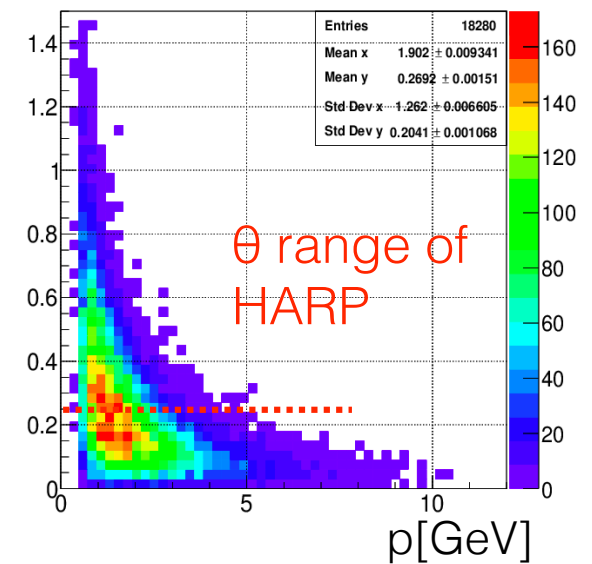
$4 < p_{in} < 8 \text{ GeV}$

$X_{out} = \pi^+$



$8 < p_{in} < 14 \text{ GeV}$

$X_{out} = \pi^+$



We need some parameterization

- to cover phase space
- to scale to different incident energy

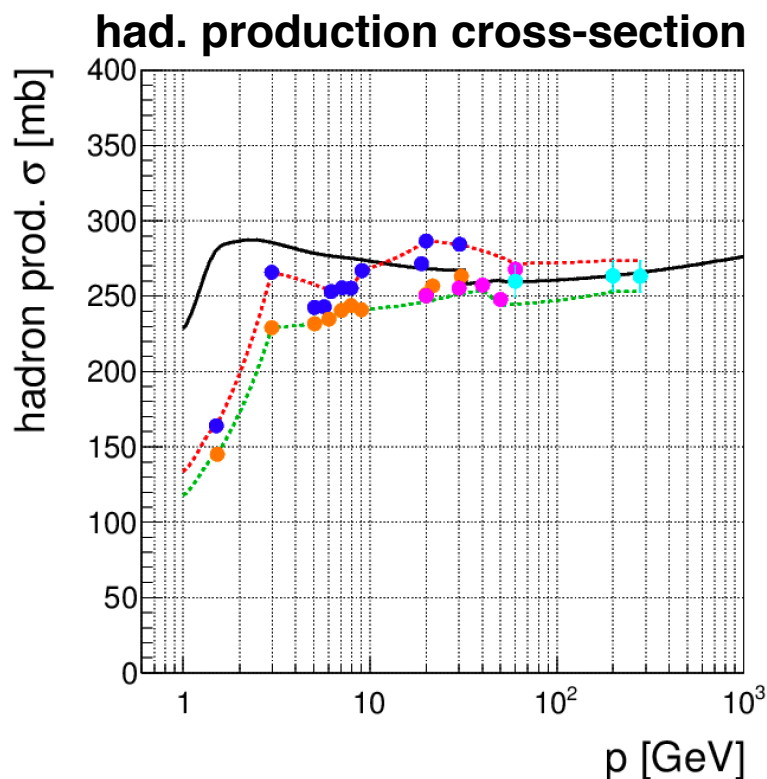
current status

apply weighting method to ATMNC

Weighting online is too time-consuming

- restore h_{in} , \mathbf{p}_{in} , h_{out} , \mathbf{p}_{out} , \mathbf{x}_{vtx} of all hadron interaction related to v hitting the detector
- apply weight at offline

Now finished to implement the weight for cross-section



ATMNC ($=\sigma_{MC}$)

p+Al data (from T2K paper [PRD 87, 012001 (2013)])

p+C data (from T2K paper [PRD 87, 012001 (2013)])

Denisov et. al. [Nucl. Phys. B61, 62 (1973)]

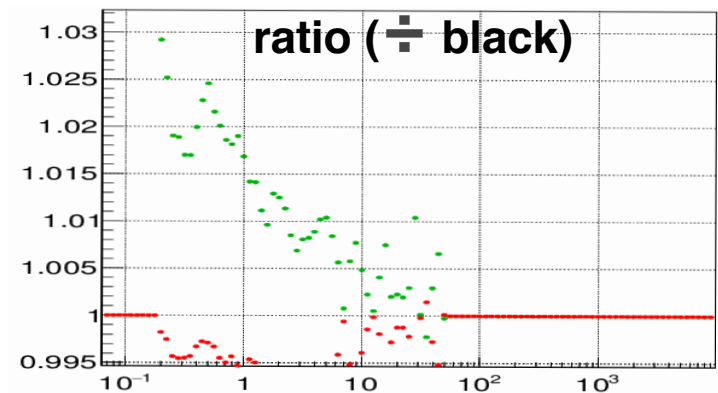
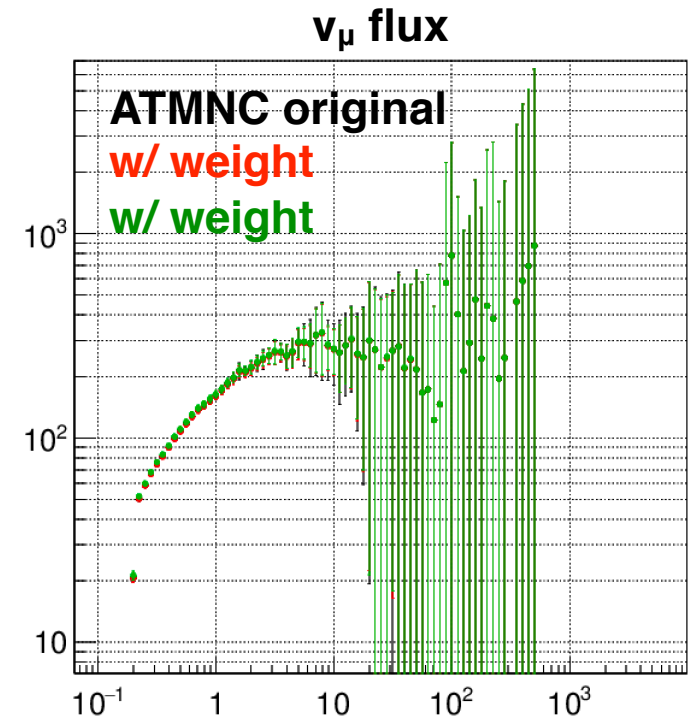
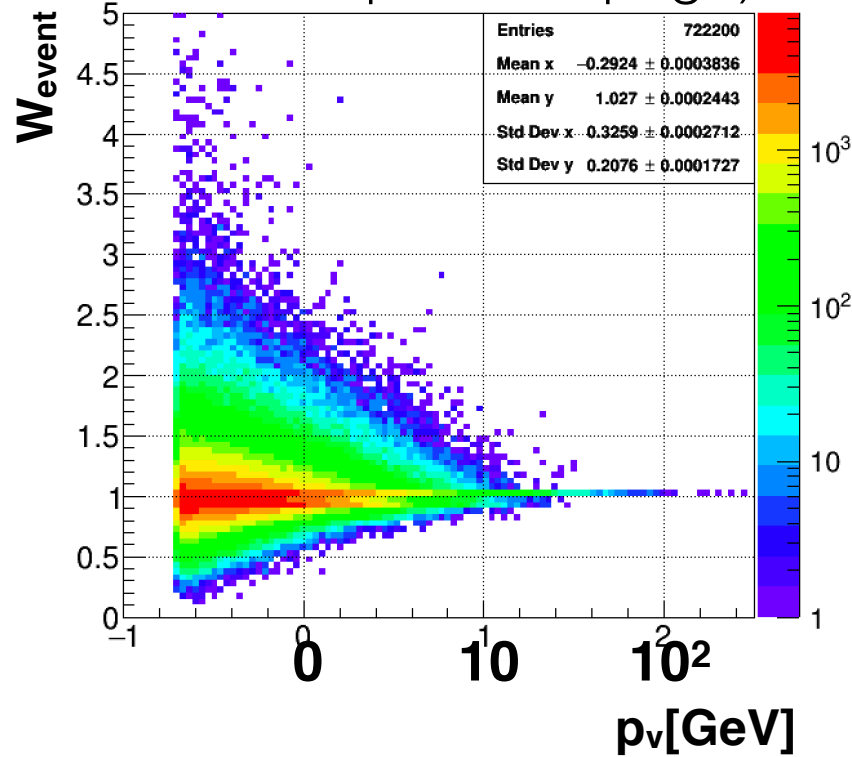
Carroll et. al. [PLB80, 3 (1979)]

--- & - - - :to calculate weight ($=\sigma_{Data}$)

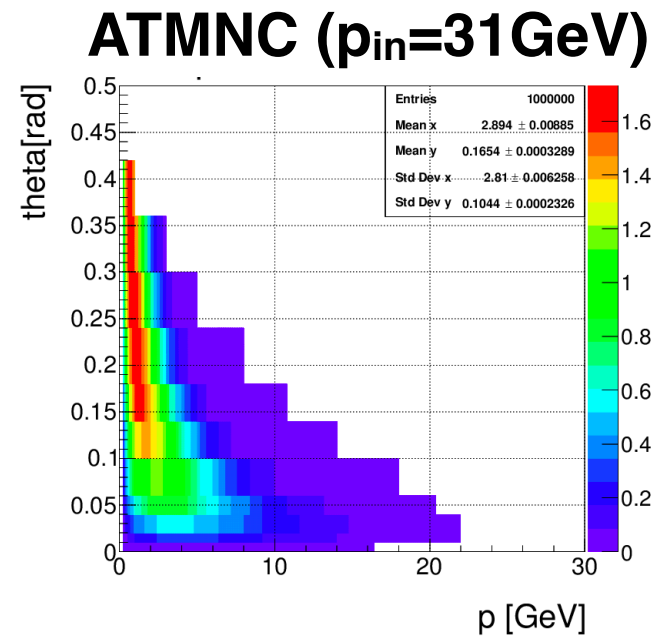
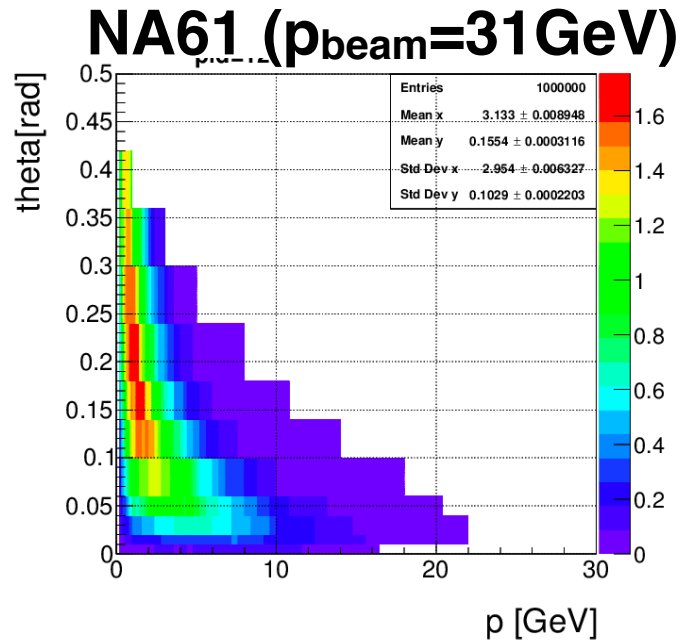
$$W = \frac{\sigma_{Data}}{\sigma_{MC}} \exp\{-L(\langle \rho \sigma_{Data} \rangle - \langle \rho \sigma_{MC} \rangle)\}$$

impact of the weight for cross-section

weight (based on the green line in the previous page)

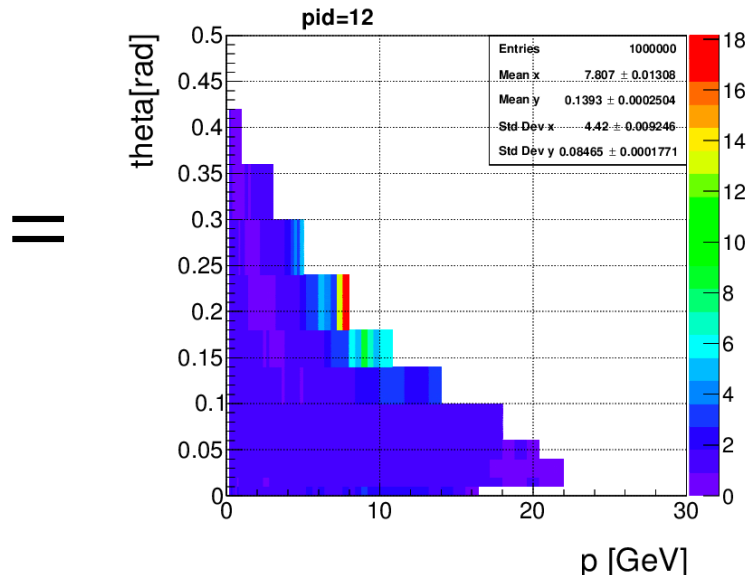


next step: weight for p - θ



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Weight table (NA61 / ATMNC)



||

to do (in the next 1-2 months)

- make tables for HARP & BNL
- parameterization to cover shortage of measured phase space
- scale to different beam energy

Then, evaluate how the uncertainty of beam experiment measurement propagate to ν flux uncertainty.

summary

- Honda's ATMNC
 - Full & 3D simulation code to calculate atm. ν flux
 - inclusive hadron interaction for speed up
 - main uncertainty comes from hadronic interaction
- activity of Nagoya group
 - incorporate the beam measurement for hadron production into ATMNC
 - implementing T2K-style weight
 - enables common treatment of the sys. uncertainty of hadronic interaction between T2K and SK
- current status
 - check the required phase space
 - implement the weight for cross section
 - now preparing the weight for p - θ distribution